StegoNPR: Information Hiding in Painterly Renderings

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Abstract
We present a novel steganographic technique for concealing information within an image. Uniquely we explore the practicality of hiding, and recovering, data within the pattern of brush strokes generated by a non-photorealistic rendering (NPR) algorithm. We incorporate a linear binary coding (LBC) error correction scheme over a raw data channel established through the local statistics of NPR stroke orientations. This enables us to deliver a robust channel for conveying short (e.g. 30 character) strings covertly within a painterly rendering. We evaluate over a variety of painterly renderings, parameter settings and message lengths.


1. Introduction
The stylization of photographs into synthetic artwork is a fundamental research problem in Non-photorealistic Rendering (NPR) [KCW112]. Painterly rendering has received considerable scrutiny, and is predominantly tackled through stroke based rendering (SBR) processes. In SBR, virtual brush strokes are composited on canvas with attributes (such as colour and orientation) driven by the underlying image content [Hae90]. In classical SBR models [Hae90, Lit97, Her98, CH02, CH05], stroke attributes are derived locally from a few pixels, whilst the spatial extent of a brush stroke is often tens of pixels. This leads to a non-linear distortion effect that, given carefully chosen stroke placement heuristics, results in an aesthetically pleasing painterly appearance.

In this paper we propose a novel use for SBR; that of concealing information within the pattern of strokes laid down during the painterly rendering process. As such we propose SBR as a novel channel for steganography — covert communication over an existing communication channel. Steganography has been explored in digital formats such as audio, ASCII text, network packets, as well as in images. In all cases the intention is for the sender to embed a second signal, robustly and imperceptibly within the carrier channel, that may be subsequently extracted by the recipient. Often as the volume of embedded data increases, distortion becomes observable within the carrier signal. We suggest painterly rendering — a process that intentionally introduces image distortion for the purpose of aesthetics — to be well suited for steganography, as this distortion serves to mask the embedded signal. To the best of our knowledge, NPR as a steganographic medium has not been previously explored.

Our algorithm is a variant of Hertzmann’s curved brush painterly rendering algorithm [Her98]. We embed covert information by quantizing the orientation of spline strokes to create differing patterns of alignment within defined regions of the painting. This permits several hundred binary digits to be reliably embedded as raw data within a typical painting. Within the resulting raw data channel, a linear binary code (LBC) provides error correction resulting a robust channel capable of carrying around 30 characters (e.g. a short message or URL) in a 1080 × 768 resolution painting.

2. Related Work
Steganography (Greek etymology: ‘secret writing’) dates back millennia to wax covered messages inscribed on tablets, and missives inked upon couriers’ skin underneath clothing. Digital steganography has evolved from this concept, often concealing messages within the carrier (cover text) signal within components that are information rich but create little or no perceptible change when altered. Examples for text documents include white-space [Kwa13], or invisible Unicode sequences used to delimit Arabic text [MJF97]. Flow control bits have been used to covertly communicate a secondary data channel over TCP/IP packets [DGPP10]. Spread
3. Steganographic Painterly Rendering

We first describe how an RGB colour image $I$ is converted into a painting $P$, as a function of pixel colour $I(x,y)$, lo-

cal gradient magnitude $|\nabla I(x,y)| = \left( \frac{\partial I}{\partial x}^2 + \frac{\partial I}{\partial y}^2 \right)^{\frac{1}{2}}$ and local gradient orientation $\Theta(x,y) = \arctan \left( \frac{\partial I}{\partial y} / \left| \frac{\partial I}{\partial x} \right| \right)$. We use notation $M = \{m_1, ..., m_n\}$ to indicate the raw data bits $m_i = \{0, 1\}$ we wish to embed within $P$.

3.1. Stroke Placement Process

We represent $P$ as a sequence of $N$ Catmull-Rom spline strokes $P = \{s_1, ..., s_N\}$ each of which comprises a variable number of 2D control points $s_j = \{e_1, ..., e_n\}$. A decision to seed a stroke is made stochastically at every pixel $p_i = \{e_1\}$; the probability of seeding a stroke at any given point is proportional to the high frequency content present at that location.

$$p(s|e_1) \propto |\nabla I(e_1)|.$$

If seeded, a stroke proceeds to grow bi-directionally from $e_1$ in directions $\Theta(e_1) \pm \pi$; a single direction of growth is illustrated in Figure 1. Growth occurs by iteratively ‘hopping’ between pixels in the approximate direction of the local gradient orientation. Specifically, given a control point $e_j$ the subsequent control point $e_{j+1}$ is given by:

$$e_{j+1} = e_j + \left[ \frac{d \cos \theta_j}{d \sin \theta_j} \right].$$

where $d$ is a constant distance proportional to the level of detail being painted (discussed shortly) and $\theta_j$ is the angular direction of the $(j-1)^{th}$ hop:

$$\theta_j = Q(\Theta(e_j) \pm \pi; c_j),$$

where $Q(\Theta; c_j)$ is an angular quantization function local to $e_j$, used to embed information in the stroke orientations, discussed in 3.2. The ambiguity $\Theta(e_j) \pm \pi$ (illustrated as $\Theta_{1/2}$)
vs. \( \Theta_{1b} \) in Figure 1) arises due to the lack of directionality on the intensity gradient \( \left[ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right]^{T} \). The angle minimising \( |\Theta(c_j) - \Theta_{j-1}| \) is chosen.

Growth of each end of the stroke proceeds independently until one of several halting criteria are met. Specifically the strokes is terminated if:

1. Adding a new control point \( c_j \) would cause the angle between hops to exceed a threshold \( |\Theta_j - \Theta_{j-1}| > T_h \), where we use threshold \( T_h = \frac{\pi}{4} \).
2. Adding \( c_j \) would depart significantly from the mean colour of the current stroke i.e. \( |c_j - \bar{\sum}_{i=1}^{j} I(c_i)| > T_c \), where we use threshold \( T_c = 0.2 \) in a normalised RGB space.

Following Hertzmann’s coarse-to-fine painting strategy, the entire stroke placement process is iterated several times at different spatial scales. A low-pass pyramid is formed and a painting generated for the coarsest layer, after which successively finer layers are over-painted. In each case \( d \) is varied inversely proportional to the pyramid level, so that larger strokes are painted at coarser scale. In our experiments we use two octave intervals of scale. Paint strokes are rendered using the mean colour of their control points i.e. \( \frac{1}{d} \sum_{j=1}^{d} I(c_j) \) and a texture map with the appearance of brush bristles applied to enhance aesthetics.

3.2. Robust Data Embedding

Data is embedded within the painterly rendering via the angular quantization function \( Q(\Theta_j; c_j) \) within equation 3, where \( \Theta_j \) is the hop angle and \( c_j = [x_j, y_j] \) is the 2D control point location. Rather than painting a stroke with hop angles derived directly from \( \Theta(\cdot) \), \( \Theta_j \) is quantized to one of several bin intervals within \( [0, 2\pi] \). In section 4.2 we evaluate configurations using 4 and 8 angular quantization bins as the parameter governs a trade between aesthetics and robustness. An alternating pattern of set (1) and reset (0) bit labels are distributed over the angular quantization bins as indicated in Figure 2 (a).

We divide the painting canvas into a rectilinear grid producing a set of \( R = \{r_1, \ldots, r_w \times h\} \) regions, each of which offer one bit of message capacity for \( M \) i.e. \( r_1 \) encodes \( m_1 \). During the message encoding process, quantization function \( Q(\Theta_j; c_j) \) determines the spatial region in which \( c_j \) falls. The quantization of \( \Theta_j \) is performed against bins labelled as matching \( m_j \). Thus in an 8 bin quantization scheme, \( \Theta_j \) will be quantized into a value drawn from one of two angle sets \( \{0, \frac{\pi}{4}, \frac{3\pi}{4}, \pi\} \) or \( \{\frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}\} \) more concisely:

\[
Q(\Theta_j; c_j) = \frac{1}{4}m_j + 2\pi \min \left\{ \frac{m_j + 2\pi i}{4} \mid i \in \mathbb{Z} \right\}, \tag{4}
\]

where \( i \) is determined by spatial quantization of \( c_j \) into the closest grid region \( r_i \). In practice it is desirable to perform angular quantization only a fraction of the grid cell, leaving

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure2.png}
\caption{Data embedding strategy. (a) The canvas is spatially divided into a grid of regions. Each region is assigned a bit of the message (following transformation of the raw message into a robust stream via Hamming coding). The bit determines the angular quantization \( Q(\cdot) \) of hops made during stroke construction. (b) grid cells are interspersed with regions on non-quantized stroke orientation which can mitigate against perceptual regularity of a tighter gridding strategy (c).}
\end{figure}

the remainder with ‘natural’ stroke orientations to mitigate against pattern artifacts arising from the regularity of strokes Figure 2 (b,c).

3.2.1. Error Correction

The bit stream \( M \) can carry any data, and so it is straightforward to robustify the data embedding using a forward error correcting (FEC) code. FEC extends a bitstream by embedding additional parity bits introducing a data redundancy that enables detection and correction of errors (bit flips). Since \( M \) is a predefined constant length \( w \times h \) in our application, we must sacrifice some capacity for robustness when using FEC.

A number of robust FEC schemes exist, for example Reed-Solomon coding used in digital communications and CDROMs. Whilst robust, many such algorithms cannot operate efficiently over the few tens of characters message length offered by our channel. We therefore opt for a linear binary coding system (LBC), specifically a Hamming code, in which consecutive groups of \( k \) bits within \( M \) are represented by \( 2^k \) codewords of bit length \( n \) in the encoded message \( M' \). Hamming codes are referred to in triplet nota-
tion (n,k,d) where d indicates the minimum Hamming distance between any of the $2^n$ codewords. Crucially, a Hamming code is able to detect up to $k/2$ errors (the ‘syndrome’) and correct up to $(k/2) - 1$ errors in a Hamming coded bit stream. Detection is performed by observing codewords in the bit stream that are not part of the codebook. Correction is performed by identifying the closest valid codeword to the received codeword, in terms of Hamming distance i.e. bit flips required to transform one into the other.

Hamming codes can be discovered through exhaustive search — we use a (7,4,3) code for our system, resulting in a 42.8% reduction in capacity but the ability to correct up to 12.5% errors in the stream. The codebook for our (7,4,3) code is \{0, 113, 98, 19, 84, 37, 54, 71, 56, 73, 90, 43, 108, 29, 14, 127\}.

3.3. Decoding Process

Given the image of a painting $P$, and knowledge of the levels of spatial (grid) and angular quantization used during data embedding, the concealed bit stream $M$ of spatial (grid) and angular quantization used during data embedding is analysed by analysing the orientations of rendering primitives in $P$. As it is challenging to segment individual primitives, which are often textured for aesthetic effect, we instead recover the orientations of stroke outlines using low-level signal processing operations.

First, the gradient magnitude and orientation are computed from the painting yielding $\nabla P(x,y) = \left(\frac{\partial P}{\partial x}^2 + \frac{\partial P}{\partial y}^2\right)^{\frac{1}{2}}$ and local gradient orientation $\Theta'(x,y) = \text{atan}\left(\frac{\partial P}{\partial x}/\frac{\partial P}{\partial y}\right)$. The objective is to recover a histogram of gradient orientations from pixels within each grid cell, the peak of which corresponds to the predominant gradient orientation and so directly to the relevant bit in the embedded data stream. To increase the signal to noise ratio within this histogram, pixels contribute only if their gradient magnitude exceeds a threshold (in our experiments, 15% of the maximum possible gradient magnitude). Figure 3 illustrates the importance of thresholding the edge map to create a unimodal distribution in the histogram and good signal to noise ratio.

4. Results and Discussion

We evaluate our system using five Creative Commons images (Figure 6a) containing varying levels of high frequency detail. The image resolution in all cases is $1080 \times 768$ pixels. We experiment with two angular quantization levels (4 and 8), and grid configurations suitable for storing messages of various lengths with and without error correction.

4.1. Qualitative Results

Figure 6 presents the results of embedding an identical 30 8-bit ASCII message within five paintings (with error correction). The length of the embedded data is 420 bits with correction (240 raw data bits). Figure 6c,d embed the image using the default angular quantization level of 8. The messages is exactly recoverable in both cases. Figure 6c illustrates that a bump map (inset) may be applied to strokes (after [Her02]) in addition to texture mapping, with the message remaining recoverable after the process. Figures 6b,d,e embed the message using a quantization level of 4. An increased regularity is observed in the stroke patterns at this quantization level.

4.2. Quantifying robustness vs. capacity

The benefits of the LBC error correction was evaluated by embedding five messages of varying bit lengths (40, 88, 144, 176, 240) within the 5 test paintings, and attempting to recover the information. The angular quantization level was 4. The test was repeated with and without error correction (Figure 5a,b respectively). In all cases where corruption occurred, error correction was shown to minimise data loss. With error correction enabled only two paintings exhibited data corruption, in the worst case 3 bits of 240 i.e. a loss rate of 1.25%.

The experiment was repeated with an angular quantization level of 8. Figure 5c indicates a higher error rate, at the cost of improved aesthetics through an improved gamut of stroke orientations (compare stroke placement in Figure 4). In both cases the Kitchen image exhibited greater error at higher capacities, possibly due to the image exhibiting larger expanses.
of flat texture. Flat texture is likely to be problematic since the colour of neighbouring strokes will be similar, and thus a stroke edge (from which orientation may be recovered) is less likely to manifest in the generated painting.

A final experiment emulated a StirMark attack by scaling the data embedded painting by 10% and 20% in Photoshop prior to decoding. No corruption was observed. When error correction was disabled, very little corruption occurred at 10% with an average of 1.6 bits dropped. At 20% the decoder, again with error correction disabled, dropped an average of 0.75 bits. We conclude that any resampling artifacts introduced are comfortably corrected by the Hamming coding scheme.

5. Conclusion

We have presented a novel form of steganography: concealing information with the output of a painterly rendering algorithm. To the best of our knowledge this is the first time the intentional aesthetic distortions of an image-based NPR algorithm have been used to conceal information. Utilising a simple Hamming coding scheme for error correction over our covert channel, we have demonstrated the ability to robustly store up to 30 characters (240 bits) within a single megapixel image. We have demonstrated that output aesthetics (fidelity of stroke orientation) may be traded for robustness and/or capacity by varying the level of angular quantization in the algorithm.

Potential avenues for further development include more sophisticated Computer Vision techniques to isolate strokes during decoding, thereby offering greater resilience to image alteration and potentially greater capacity. The finest grid size tested featured cells of size approximately 50 × 25 (for 240 error corrected bits = 420 raw bits). This is approaching the resolution of the larger individual brush strokes. The ability to robustly isolate brush strokes for analysis (perhaps of their medial axis) might improve the handling of smaller strokes and so an increase in the maximum practical grid resolution for data embedding.

References


Figure 6: A gallery of steganographic paintings (b-f): Ruins, Causeway, Jungle, Kitchen, Charles, generated from the corresponding five photographs (a) using our method under various experimental configuration. The 30 character 8-bit ASCII message ‘This is a longer test message!’ has been embedded in all paintings. See section 4 for further discussion.

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