

Advanced Illumination Techniques for GPU-Based Volume Raycasting

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Scattering Effects

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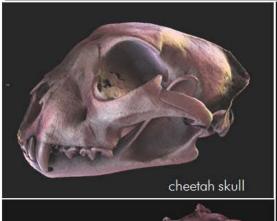


Timo Ropinski Visualization and Computer Graphics Research Group,

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Advanced Illumination





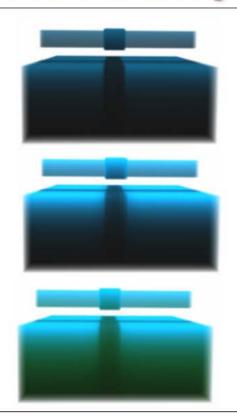


Data sets available at the UTCT data archive, DIGIMORPH http://utct.tacc.utexas.edu

ADVANCED ILLUMINATION TECHNIQUES FOR GPU-BASED VOLUME RAYCASTING



Translucency





Light Transport

Wave-Particle Duality

Photons

- Quantum of light (the smallest possible packet of light at a given wavelength)
- Photoelectric effect (van Lenard, 1902)

Wave Theory (Maxwell)

- Electro-magnetic wave characteristics of light
- Effects such as interference and diffraction

Quantum Mechanics (Einstein)

- Universal theory of light transport
- probabilistic characteristics of the motions of atoms and photons (quantum optics)

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Light Transport

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Scattering Effects Single and Multiple Scattering

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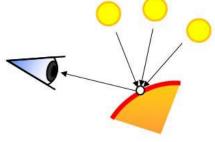
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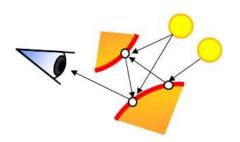


Scattering Effects

When a photon hits a surface, it changes both direction and energy

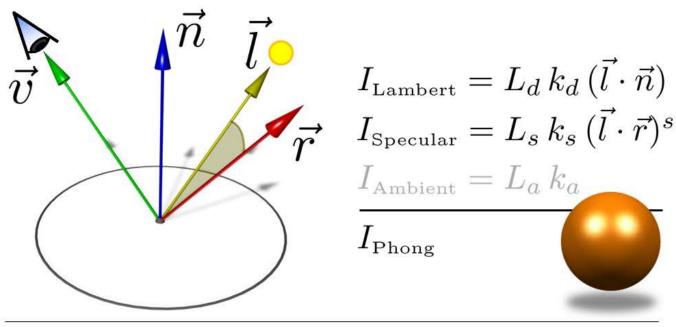
- Single Scattering:
 - Light is scattered once before it reaches the eye
 - Local illumination model
- Multiple Scattering
 - Soft shadows
 - Translucency
 - Color bleeding





Single Scattering

Phong illumination with point light sources

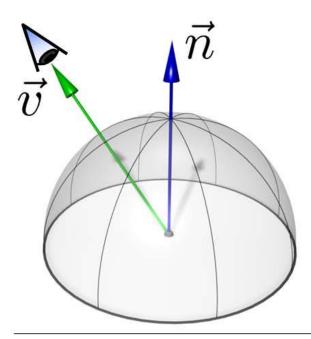


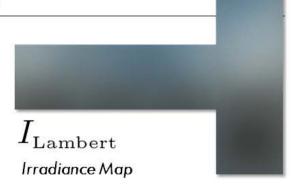
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Single Scattering

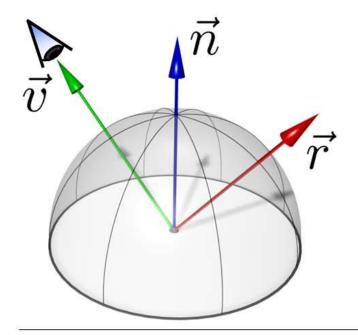
Environment Light

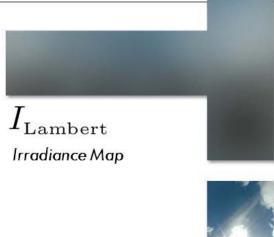




Single Scattering

Environment Light





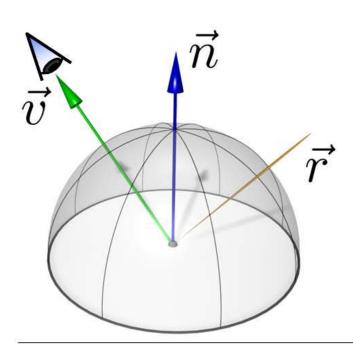


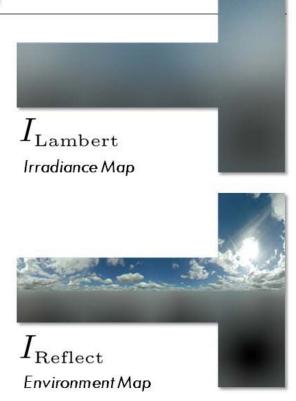
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Single Scattering

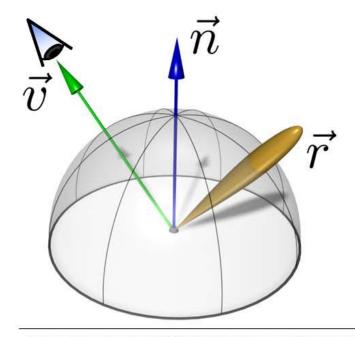
Environment Light

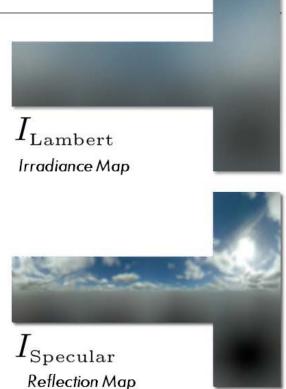






Environment Light



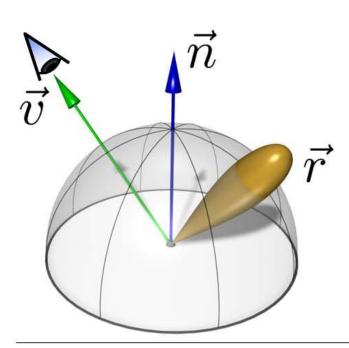


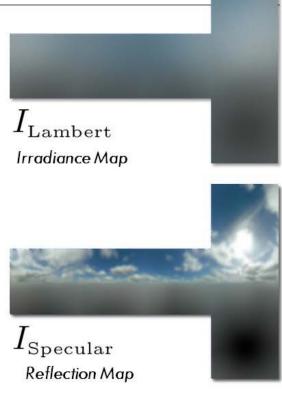
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Eurographics 2009



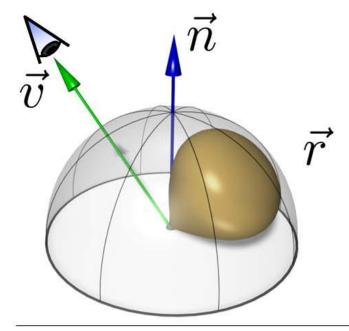
Environment Light

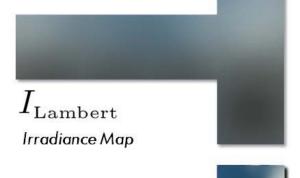




Single Scattering

Environment Light







ADVANCED ILLUMINATION TECHNIQUES FOR GPU-BASED VOLUME RAYCASTING





Math Notation





Hemisphere

BRDF

Elevation Angle

Volume Illumination

$$L(\mathbf{x}, \omega_o) = \int_{\Omega} p(\mathbf{x}, \omega_o \to \omega_i) d\omega_i$$

Sphere

Phase Function



Scattering Effects Monte-Carlo Methods

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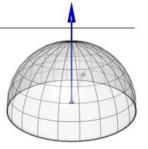
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Math Notation

Mathematical Model

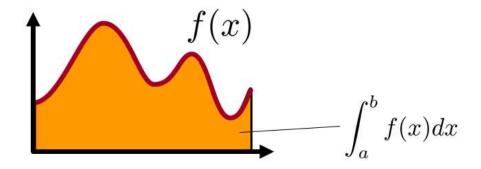
$$L(\mathbf{x}, \omega_o) = \int_{\Omega} p(\mathbf{x}, \omega_o \to \omega_i) L(\mathbf{x}, \omega_i) d\omega_i$$



integrates over the entire sphere/hemisphere

- Integral must be solved for every intersection point
- Fredholm Equation (cannot be solved analytically)

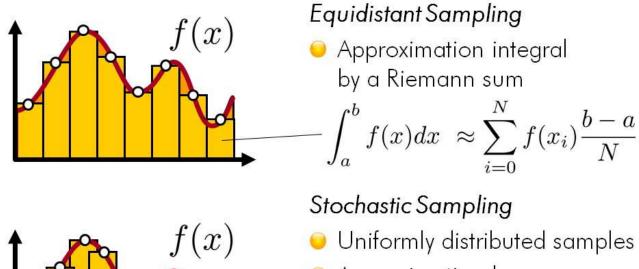
Numerical Integration

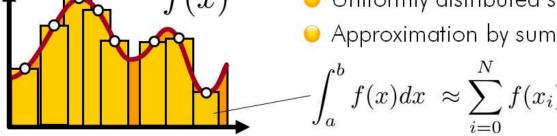


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Numerical Integration

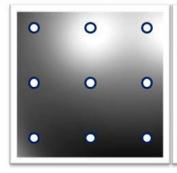


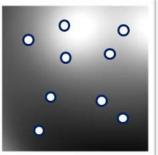


Stochastic Sampling

Cons:

 Slower convergence than Riemann sum





Pros:

Better Scalability for multidimensional functions: increase number of samples in arbitrary steps

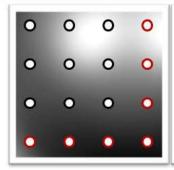
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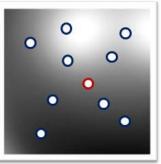


Stochastic Sampling

Cons:

 Slower convergence than Riemann sum





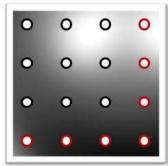
Pros:

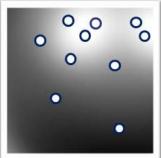
• Better Scalability for multidimensional functions: increase number of samples in arbitrary steps

Stochastic Sampling

Cons:

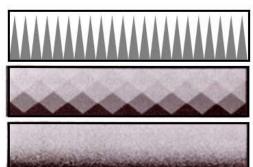
 Slower convergence than Riemann sum





Pros:

- Better Scalability for multidimensional functions: increase number of samples in arbitrary steps
- Noise instead of Aliasing
- Independent of sampling grid: Clever placement of samples will improve the convergence!



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Blind Monte-Carlo Sampling

Example: Filtering an Environment Map

Given an Environment Map

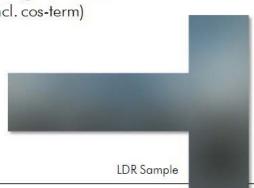
(i.e. photograph: fisheye or mirror ball)

Calculate an Irradiance Map

For each pixel of the irradiance map:

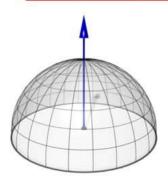
- Determine n random directions on the hemisphere
- Sample the Environment Map and
- Average the results (incl. cos-term)





Rendering

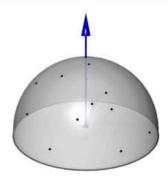
- Calculate the radiance from a point
 - depending on the incoming light on the sphere/hemisphere
 - depending on the phase function/BRDF



Deterministic

Uniform sampling of the sphere/hemisphere.

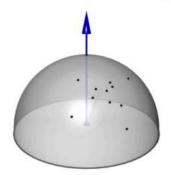
High computational load good approximation



Blind Monte-Carlo

Randomized sampling of the sphere/hemisphere.

Visually better images for fewer samples, slow convergence



Importance Sampling

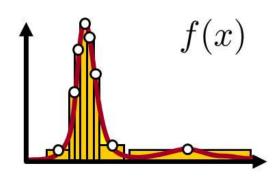
Place samples where contribution is high

Faster!

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Importance Sampling



Stochastic Sampling

- Non-uniformly distributed samples
- Approximation by sum

$$\int_{a}^{b} f(x)dx \approx \sum_{i=0}^{N} \frac{f(x_i)}{p(x_i)}$$

Clever placement of samples

- Many samples where function is high
- Few samples where function is low

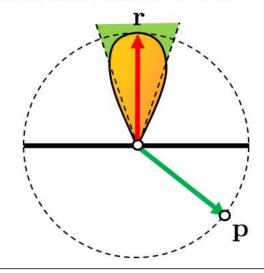
Probability Distribution Function (PDF)

Sampling a Specular Lobe

Simple Approach

Specular term $f(\varphi) = \cos^s(\varphi) = (\mathbf{r} \cdot \mathbf{v})^s$ Non-optimal, but easy to implement *Idea*: uniform distribution of directions restricted to a cone

- Precompute random unit vectors with uniform PDF
- Randomly pick one vector p



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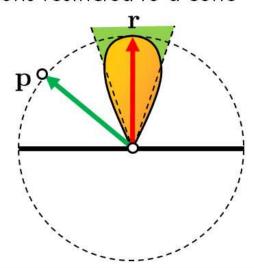


Sampling a Specular Lobe

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- Precompute random unit vectors with uniform PDF
- Randomly pick one vector p
- Negate vector, if $(\mathbf{r} \cdot \mathbf{p}) < 0$



Sampling a Specular Lobe

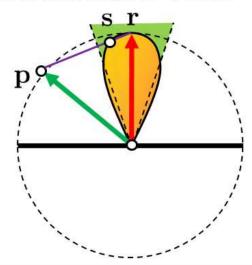
Simple Approach

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Idea: uniform distribution of directions restricted to a cone

- Precompute random unit vectors with uniform PDF
- Randomly pick one vector p
- ullet Negate vector, if $({f r}\cdot{f p})<0$
- Blend with vector r and normalize

$$\mathbf{s} = \alpha \, \mathbf{r} + (1 - \alpha) \mathbf{p}$$



ADVANCED ILLUMINATION TECHNIQUES FOR GPU-BASED VOLUME RAYCASTING



Sampling a Specular Lobe

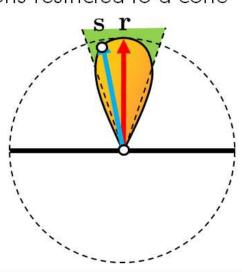
Simple Approach

Specular term $f(\varphi) = \cos^s(\varphi) = (\mathbf{r} \cdot \mathbf{v})^s$

Non-optimal, but easy to implement

Idea: uniform distribution of directions restricted to a cone

- Precompute random unit vectors with uniform PDF
- Randomly pick one vector p
- ullet Negate vector, if $({f r}\cdot{f p})<0$
- Blend with vector \mathbf{r} and normalize $\mathbf{s} = \alpha \mathbf{r} + (1 \alpha)\mathbf{p}$
- Blend weight α controls the size
 of the specular highlight and can
 be calculated from shininess s



Stochastic Sampling

$$\int_{a}^{b} f(x)dx \approx \sum_{i=0}^{N} \frac{f(x_i)}{p(x_i)}$$

- What is the *ideal PDF* for sampling a given function f(x)?
- Variance is minimal, if

$$p(x) = \lambda \cdot f(x)$$

- ullet λ must be chosen to normalize the distribution
- Problem:

$$\int_{a}^{b} p(x)dx = 1 \quad \Rightarrow \quad p(x) = \frac{f(x)}{\int_{a}^{b} f(x)dx}$$

The ideal PDF requires knowing the integral beforehand!

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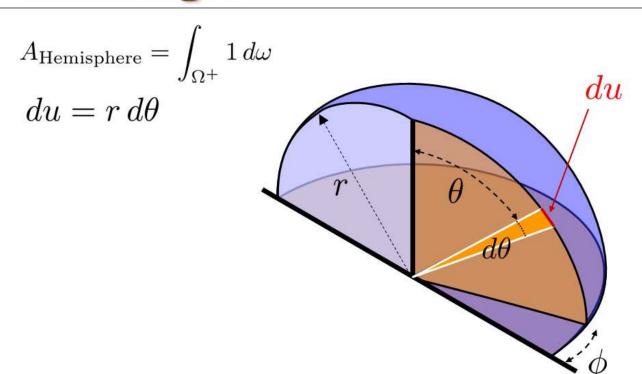
Stochastic Sampling

$$L(\mathbf{x}, \omega_o) = \int_{\Omega} f(\mathbf{x}, \omega_i \to \omega_o) L(\mathbf{x}, \omega_i) \cos \theta_i d\omega_i$$
known

Although we do not know the integral completely, we still know parts of it

$$\hat{p}(\omega_i) = f(\mathbf{x}, \omega_i \to \omega_o) \cos \theta_i$$
$$p(\omega_i) = \frac{\hat{p}(\omega_i)}{\int_{\Omega} \hat{p}(\omega) d\omega}$$

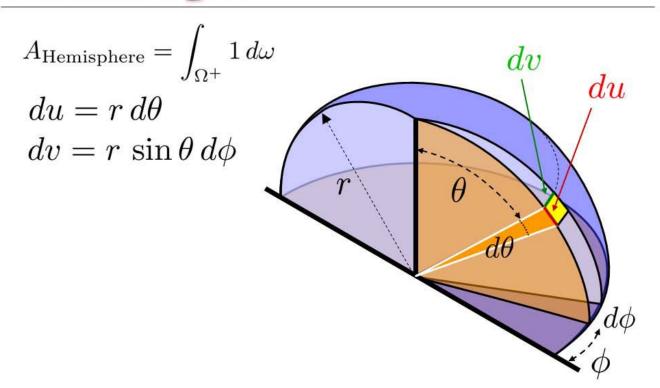
Solid Angle



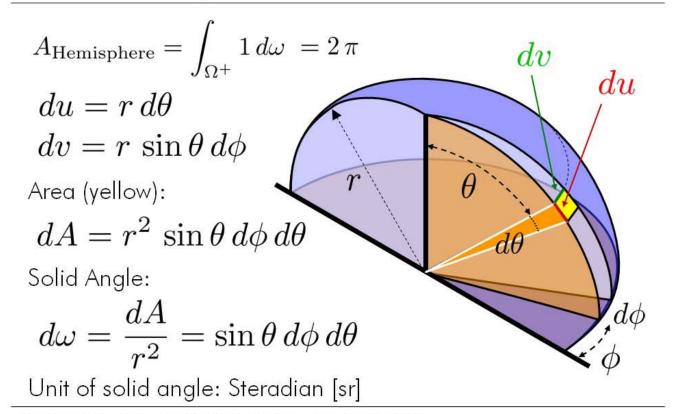
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Solid Angle



Solid Angle



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Sampling a Specular Lobe

Ideal Sampling

$$f(\omega_i) = \cos^n(\theta_i)$$

$$p(\omega_i) = \frac{f(\omega_i)}{\int_{\Omega^+} f(\omega_i) d\omega}$$

$$\int_{\Omega^+} \cos^n(\theta) d\omega = \int_0^{2\pi} \int_0^{\pi/2} \cos^n(\theta) \sin(\theta) d\theta d\phi = \frac{2\pi}{(n+1)}$$

Sampling a Specular Lobe

Ideal Sampling

$$f(\omega_i) = \cos^n(\theta_i) \qquad p(\omega_i) = \frac{f(\omega_i)}{\int_{\Omega^+} f(\omega_i) d\omega}$$
$$p(\theta_i, \phi_i) = \frac{(n+1)}{2\pi} \cos^n \theta_i \sin \theta_i$$
$$p(\theta_i) = (n+1)\cos^n \theta_i \sin \theta_i \qquad p(\phi_i|\theta_i) = \frac{1}{2\pi}$$

Convert to CDF and invert

$$\theta_i = \cos^{-1} \xi_1^{\left(\frac{1}{n+1}\right)} \qquad \qquad \phi_i = 2\pi \xi_2$$

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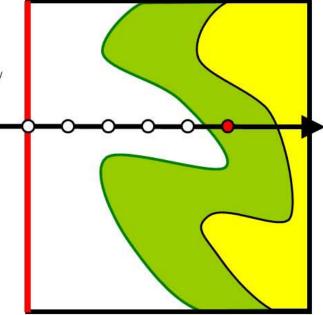
Importance Sampling

Literature:

- M. Pharr, G. Humphries: **Physically Based Rendering**, Morgan Kauffman (Elsevier), 2004
- M. Colbert, J. Křivánek, **GPU-Based Importance Sampling** in H.Nguyen (edt.): **GPU Gems 3**, Addison-Wesley, 2008

GPU Ray-Casting

- Calculate First Intersection with Isosurface
- Rasterize the front faces of the bounding box
- For each fragment, cast a ray
- Find first intersaction point with isosurface by sampling along the ray

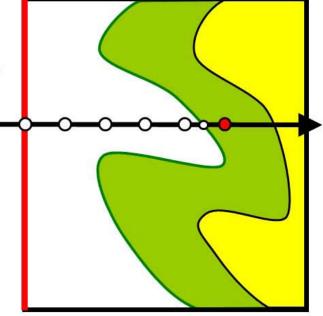


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GPU Ray-Casting

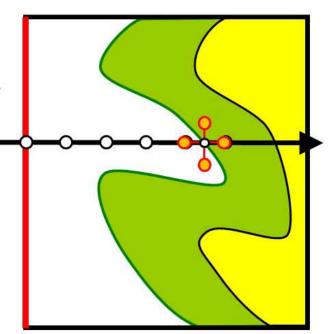
- Calculate First Intersection with Isosurface
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 - interval bisection



GPU Ray-Casting

Calculate First Intersection with Isosurface

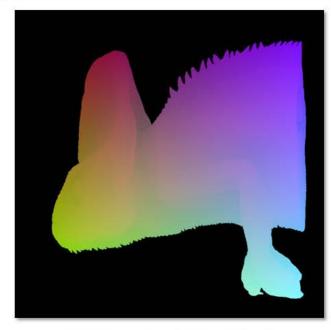
- Rasterize the front faces of the bounding box
- For each fragment, cast a ray
- Find first intersaction point with isosurface by sampling along the ray
 - interval bisection
- Store the intersection point in render target 0
- Estimate the gradient vector using central differences
- Store the gradient vector in render target 1



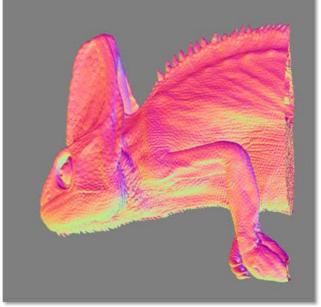
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First Render Pass



MRTO: xyz-coordinates of first intersection point with isosurface



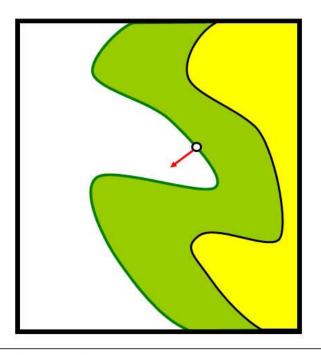
MRT1: xyz-components of gradient vector (color coded)

Deferred Shading

Single Scattering (no shadows)

- Diffuse term:
 - Sample irradiance cube using gradient direction





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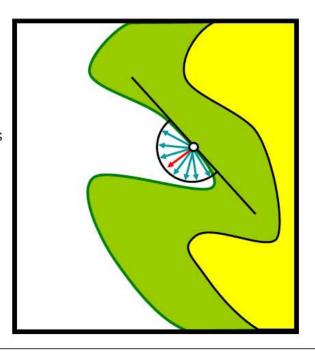


Deferred Shading

Single Scattering (no shadows)

- Diffuse term:
 - Sample irradiance cube using gradient direction
- Specular term:
 - Calculate random directions on the specular lobe
 - Sample environment cube



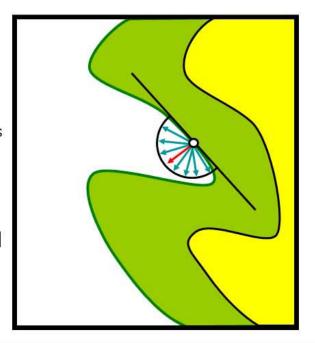


VOLUME RAYCASTING

Deferred Shading

Single Scattering (no shadows)

- Diffuse term:
 - Sample irradiance cube using gradient direction
- Specular term:
 - Calculate random directions on the specular lobe
 - Sample environment cube
 - Weight each sample with its BRDF/phase function and its probability distribution



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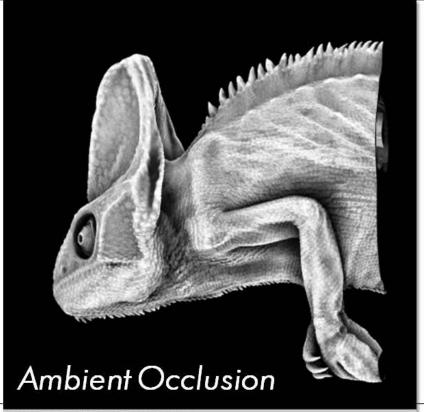


High Quality Isosurface



High Quality Isosurface

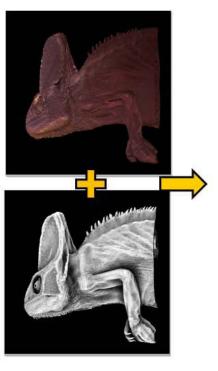




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High Quality Isosurface





ADVANCED ILLUMINATION TECHNIQUES FOR GPU-BASED VOLUME RAYGASTING

Our First Implementation

Why not use a pre-filtered environment map?

You can, but

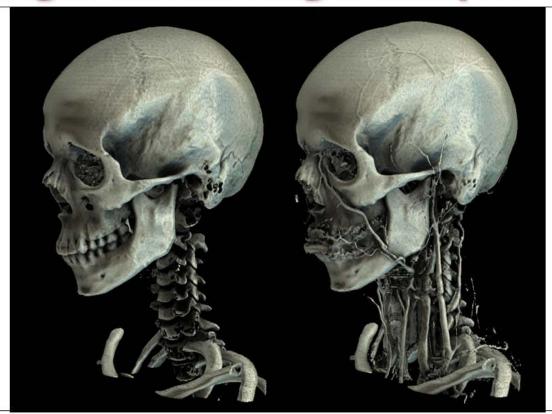
- it only works for one specular exponent per object
- Variable shininess may be used to visualize additional surface properties (e.g. gradient magnitude)



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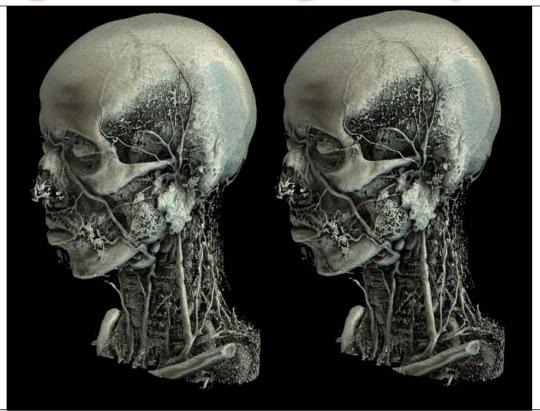
Single Scattering Example



ADVANCED ILLUMINATION TECHNIQUES FOR GPU-BASED VOLUME RAYCASTING



Single Scattering Example



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Multiple Scattering

Mathematical Model

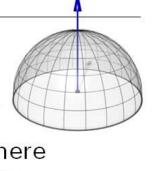
$$L(\mathbf{x}, \omega_o) = \int_{\Omega} p(\mathbf{x}, \omega_o \to \omega_i) L(\mathbf{x}, \omega_i) d\omega_i$$



- Integral must be solved for every intersection point
- Fredholm Equation (cannot be solved analytically)

Numerical Solution:

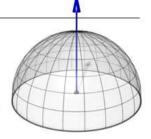
- Number of rays grows exponentially
- Much workload spent for little contribution



Multiple Scattering

Mathematical Model

$$L(\mathbf{x}, \omega_o) = \int_{\Omega} p(\mathbf{x}, \omega_o \to \omega_i) L(\mathbf{x}, \omega_i) d\omega_i$$



integrates over the entire sphere/hemisphere

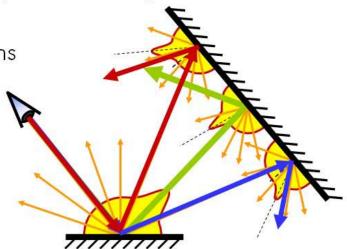
Quantum Optics

Trace the path of single photons

Photons are scattered randomly

 Probability of scattering direction given by BRDF/phase function

Monte Carlo path tracing

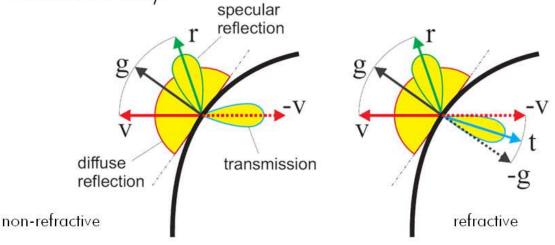


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Phase Function Model

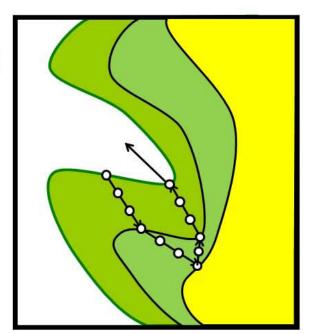
- Scattering of light at every point inside the volume
 - Too expensive (extremely slow convergence)
 - Not practicable. Controlling the visual appearance is difficult
- Idea: Restrict scattering events to a fixed number of isosurfaces only.



GPU Ray-Casting

Scattering Pass

- Start at first isosurface and trace inwards
- Account for absorption along the rays
- Proceed until next isosurface
- Calculate scattering event
- Sample the environment on exit



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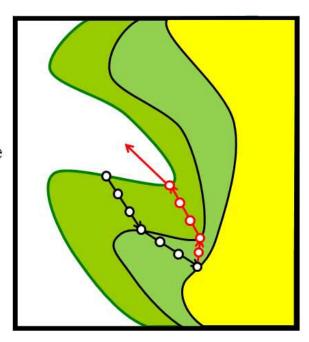


GPU Ray-Casting

Scattering Pass

Simplifying Assumption:

- Absorption on the "way in" is same as on the "way out"
- Abort the ray inside the volume square the absorption and sample irradiance map
- Not very accurate but good visual results



Scattering Pass





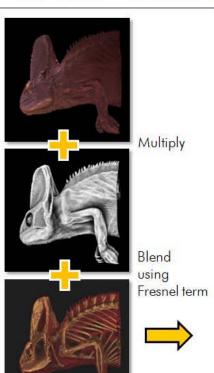
preview in real-time

final version in 1/2-1 seconds

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Final Composite





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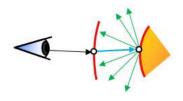
Path Tracing

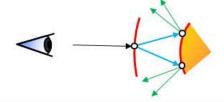
Primary rays: 1 Secondary rays: 64 Primary rays: 8 Secondary rays: 8 Primary rays: 64 Secondary rays: 1

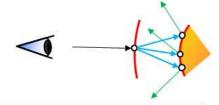










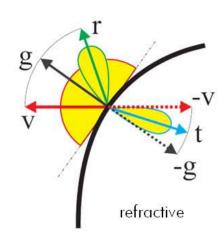


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Eurographics 2009

Examples

Different scattering cone angles for the "inward-looking" (transmissive) Phong-lobe







Scattering Effects Light Map Approaches

Markus Hadwiger VR VIS Research Center Vienna, Austria



Patric Ljung Siemens Corporate Research Princeton, NJ, USA



Christof Rezk Salama Computer Graphics Group Institute for Vision and Graphics

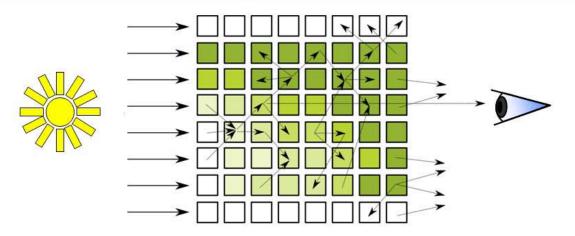
University of Siegen, Germany



Timo Ropinski Visualization and Computer Graphics Research Group, University of Münster, Germany



3D Light Map



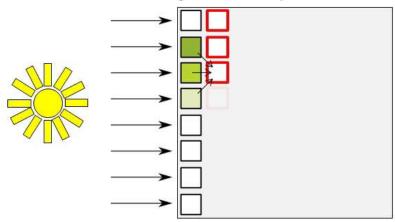
- Direct light by shadow volume or deep shadow map
- Consider the exchange of radiant energy between neighbouring voxels
- Approximate by blur operation (like [Kniss, 2002])



Generate a 3D Light Map

Based on Shadow Volume

- Calculate shadow volume for direct light as in
 - U. Behrens and R. Ratering. Adding Shadows to a Texture-Based Volume Renderer. In Proc. IEEE Symposium on Volume Visualization, 1998, p.39–46.
- Blur the direct light slice by slice





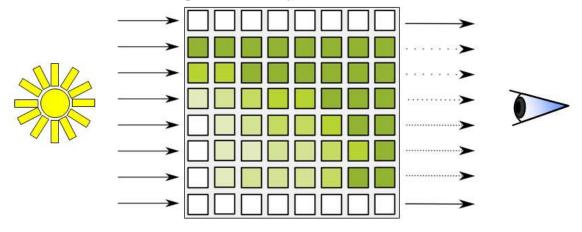
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Generate a 3D Light Map

Based on Shadow Volume

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- Blur the direct light slice by slice



Scattering 3D Light Map

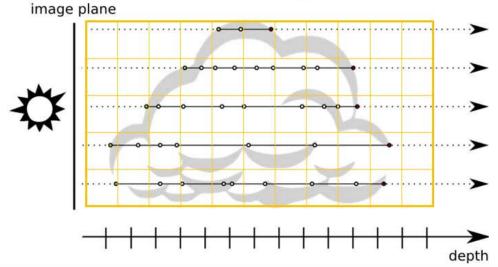


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Calculate a 3D Light Map

- Based on Deep Shadow Map
- Resample the deep shadow map on a uniform voxel grid
- Coarse grid resolution is sufficient due to the low-frequent nature of volumetric scattering



Scattering Deep Shadow Map

Direct light



Direct plus indirect light

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Light Map Approaches

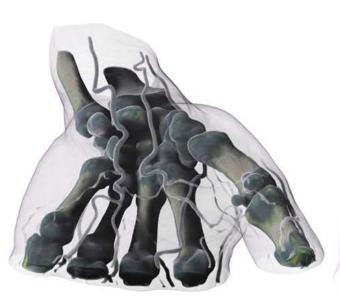
Shadow Volume Appraoch

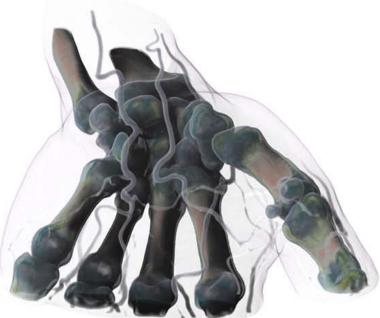
- Calculated in Model Space
 - Limited by Resolution of Shadow Volume
- High Memory Requirements

Deep Shadow Map Appraoch

- Calculated in Screen Space
 - Limited by Resolution of Shadow Volume
- Reduced Memory Requirements
- High Precision

High Dynamic Range





Direct light and shadows

Direct light, shadows and translucency

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Summary

Scattering Effects

- Single Scattering
 - Filtered Environment Maps
 - Monte-Carlo Integration

Multiple Scattering

- Monte-Carlo Integration
- 3D Light Maps (Shadow Volume/Deep Shadow Map)



Acknowledgements

- Images and Slides on Deep Shadow Maps: Andrea Kratz, Zuse Institute, Berlin Markus Hadwiger, VRVis, Vienna
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 - Medical data sets courtesy of Agfa Vienna and Dept. Of Neurosurgery, Medical University Vienna
 - Chameleon, Cheetah, Bat, Pterosaur courtesy of UTCT data archive, University of Texas at Austin
 - Carp Data set courtesy of Univ. of Erlangen-Nuremberg

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