# Supplemental Material: FAKIR : An algorithm for revealing the anatomy and pose of statues from raw point sets 

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#### Abstract

This supplemental material provides mathematical details for computing the distance and projection of a point onto a bone, and the optimization details for bone and joint parameters as they are performed in the FAKIR algorithm. It also provides additional FAKIR registration results and comparisons between registration obtained through our sequential optimization and a direct simultaneous optimization.


## A. One-bone distance computation

In this appendix, we detail the projection of a point $p$ on a bone $B$ given an approximation of the oriented normal of point $p$. Instead of using the usual orthogonal projection on the bone, we constrain the projection $\tilde{p}$ to have a normal coherent with the one of $p$. This constraint is helpful when the bone lies far away from its corresponding point set: the point can then be projected on the "right side" of the bone. In the following, without loss of generality, let us assume $r_{1} \leq r_{2}$. All the following computations depend on an angle $\alpha$ defined in Fig. 1 and which can be expressed as $\alpha=\arctan \frac{\left|r_{2}-r_{1}\right|}{\sqrt{\left\|c_{1} c_{2}\right\|^{2}-\left(r_{2}-r_{1}\right)^{2}}}$. Let us first compute $p^{\star}$ the projection of $p$ on the oriented line $c_{1} c_{2}$, and two translations of these points along this line: $p_{\alpha}^{\star}$ at the distance $\left\|p p^{\star}\right\| \tan \alpha$ of $p^{\star}$ and $p_{-\alpha}^{\star}$ at the distance $-\left\|p p^{\star}\right\| \tan \alpha$, as illustrated on Figure 1. Let $\tau_{\alpha}=\frac{p_{\alpha}^{\star}-c_{1}}{c_{2}-c_{1}}$, so that $p_{\alpha}^{\star}$ can be expressed as $\tau_{\alpha} c_{1}+\left(1-\tau_{\alpha}\right) c_{2}$. Different cases can occur:

- $0<\tau_{\alpha}<1$ : the point projects on the cone part of the bone. Let $\tilde{p}_{\alpha}$ be the intersection of segment $\left[p_{\alpha}^{\star} p\right]$ with the cone. $\tilde{p}_{\alpha}$ is the orthogonal projection of $p$ on the bone. If the normal to $\tilde{p}_{\alpha}$ has a positive scalar product with the normal of $p, \tilde{p}=\tilde{p} \alpha$. Otherwise, normals are deemed inconsistent and $\tilde{p}=\tilde{p}_{-\alpha}$, i.e. the farthest intersection of $p p_{-\alpha}^{\star}$ with the non-truncated cone. This situation occurs when the point $p$ is on the wrong side of the bone (i.e. its normal is inconsistent with the normal of its closest point on the bone).
- $\tau_{\alpha}<0$ (resp. $\tau_{\alpha}>1$ ): $\tilde{p}$ is the projection of $p$ on the sphere centered at $c_{1}$ (resp. $c_{2}$ ) with consistent normal direction, except if this normal-constrained projection falls within the bone and not on the envelop. In that case, $p$ is on the wrong side of the bone, and we set $\tilde{p}=\tilde{p}_{-\alpha}$ on the other side of the non-truncated cone.

In any case, the distance between $p$ and its normal-constrained projection $\tilde{p}$ vanishes when $p$ is located near the surface of one bone, with a normal oriented consistently. It may happen that the returned projection does not provide a point belonging to the surface of the bone: on Figure $1, \tilde{q}_{-\alpha}$ is the normal-constrained projection of point $q$, but it is not on the surface of the bone. It corresponds to a case where the point is very far from the part of the bone which is coherent with its normal. During the registration process, $\tilde{q}_{-\alpha}$ will attract $q$ on the other side of the bone, so that the projection point will gradually be replaced by a more consistent one.


Figure 1: Various projection cases. $p$ has two possible projections $\tilde{p}_{\alpha}$ and $\tilde{p}_{-\alpha}$ depending on the orientation of the normal at $p$. Point $p^{\star}$ is the projection of $p$ on line $c_{1} c_{2}$. If the normal at $p$ is oriented upward $\tilde{p}=\tilde{p}_{\alpha}$. Otherwise, $\tilde{p}=\tilde{p}_{-\alpha}$. The same strategy is used to project points $q$ and $o$.

For completeness, let us express unsigned distance $d(p)=\| p-$ $\tilde{p} \|$ in the various cases since they will be required in the following

Levenberg-Marquardt optimization formulations. If $\tau_{\alpha}<0$ (resp. $\left.\tau_{\alpha}>1\right), d(p)=\left\|c_{1} p\right\|-r_{1}\left(\right.$ resp. $\left.d(p)=\left\|c_{2} p\right\|-r_{2}\right)$. If $0 \leq \tau \leq 1$ :

$$
d(p)= \begin{cases}\left\|p p_{\alpha}^{\star}\right\|-r_{\alpha}(p) & \text { if } n_{\tilde{p}} \cdot n_{p}>0  \tag{1}\\ \left\|p p_{-\alpha}^{\star}\right\|+r_{-\alpha}(p) & \text { if } n_{\tilde{p}} \cdot n_{p} \leq 0\end{cases}
$$

Since the radius of the cone varies linearly along line $c_{1} c_{2}$ :

$$
\begin{align*}
r_{\alpha}(p) & =\left\|\tilde{p_{\alpha}} p_{\alpha}^{\star}\right\|=\left(1-\tau_{\alpha}(p)\right) r_{1}+\tau_{\alpha}(p) r_{2} \\
r_{-\alpha}(p) & =\left\|p_{-\alpha} p_{-\alpha}^{\star}\right\|=\left(1-\tau_{-\alpha}(p)\right) r_{1}+\tau_{-\alpha}(p) r_{2} \tag{2}
\end{align*}
$$

with: $\tau_{\alpha}(p)=\frac{c_{1} p_{\alpha}^{\star} \cdot c_{1} c_{2}}{\left\|c_{1} c_{2}\right\|^{2}}$ and $\tau_{-\alpha}(p)=\frac{c_{1} p_{-\alpha}^{*} \cdot c_{1} c_{2}}{\left\|c_{1} c_{2}\right\|^{2}}$. Furthermore $\left\|p p_{\alpha}^{\star}\right\|=\left\|p p_{-\alpha}^{\star}\right\|=\left\|p p^{\star}\right\| / \cos \alpha$. Hence, for each bone, we first compute the $\alpha$ angle, then, for each point $p$, we compute its projection $p^{\star}$ on $c_{1} c_{2}$ and the corresponding $\tau_{\alpha}(p)$ yielding $r_{ \pm \alpha}(p)$ and $\tilde{p}_{ \pm \alpha}$.

## B. Optimization for one bone

Let us assume that $c_{1}$ (Fig. 1) is fixed and let us optimize for the pose and intrinsic parameters of bone $B$. In a local reference frame centered at $c_{1}$ with x -axis aligned with $c_{1} c_{2}, c_{1}$ has coordinates $(0,0,0)$ and $c_{2}$ has initial coordinates $(l, 0,0)$. The rotation of the bone can be parameterized by a rotation of angle $\theta_{1}$ around the $y$-axis followed by a rotation of angle $\theta_{2}$ around the z -axis. The one-bone energy is invariant by rotation around the x -axis. After the double rotation, $c_{2}$ has coordinates $\left(l \cos \theta_{2} \cos \theta_{1}, l \sin \theta_{2}, l \cos \theta_{2} \sin \theta_{1}\right)$. Let us call $(x, y, z)$ the coordinates of point $p$ in this local coordinate system and express $d(p)$ with respect to parameters $\boldsymbol{\theta}=\left(\theta_{1}, \theta_{2}\right), l$ and $\boldsymbol{r}=\left(r_{1}, r_{2}\right)$. We have:

$$
\begin{gathered}
\tan \alpha=\frac{r_{2}-r_{1}}{\sqrt{l^{2}-\left(r_{2}-r_{1}\right)^{2}}}, \cos \alpha=\frac{\sqrt{l^{2}-\left(r_{2}-r_{1}\right)^{2}}}{l} \\
\left\|c_{1} p\right\|^{2}=x^{2}+y^{2}+z^{2} \\
\left\|c_{1} p^{\star}\right\|=x \cos \theta_{2} \cos \theta_{1}+y \sin \theta_{2}+z \cos \theta_{2} \sin \theta_{1} \\
\left\|p^{\star} p\right\|^{2}=x^{2}+y^{2}+z^{2}-\left(x \cos \theta_{2} \cos \theta_{1}+y \sin \theta_{2}+z \cos \theta_{2} \sin \theta_{1}\right)^{2} \\
\left\|p^{\star} p_{\alpha}^{\star}\right\|=\left\|p^{\star} p\right\| \tan \alpha \\
\left\|p_{\alpha}^{\star} p\right\|=\frac{\left\|p^{\star} p\right\|}{\cos \alpha} \\
\tau_{ \pm \alpha}(p)=\frac{\left\|c_{1} p^{\star}\right\| \pm\left\|p^{\star} p_{\alpha}^{\star}\right\|}{l} \\
\left\|c_{2} p\right\|^{2}=\left(x-l \cos \theta_{2} \cos \theta_{1}\right)^{2}+\left(y-l \sin \theta_{2}\right)^{2}+\left(z-l \cos \theta_{2} \sin \theta_{1}\right)^{2}
\end{gathered}
$$

The one-bone energy function is (dropping the $k$ subscript for simplicity):

$$
\begin{equation*}
E(P, B(l, \mathbf{r}), \boldsymbol{\theta})=\sum_{p \in P} d(p)^{2} \tag{3}
\end{equation*}
$$

The optimization is performed on three set of parameters in turn: angles $\boldsymbol{\theta}$, bone length $l$ and bone radii $\boldsymbol{r}$.
the optimization for bone $B$ with respect to $\boldsymbol{\theta}$ writes:

$$
\begin{equation*}
\hat{\boldsymbol{\theta}} \equiv \underset{\boldsymbol{\theta}}{\operatorname{argmin}} E(P, B(l, \mathbf{r}), \boldsymbol{\theta})=\underset{\boldsymbol{\theta}}{\operatorname{argmin}} \sum_{p \in P} d(p, \boldsymbol{\theta})^{2} \tag{4}
\end{equation*}
$$

Following the Levenberg-Marquardt algorithm, at each iteration, parameter $\boldsymbol{\theta}$ is replaced by a new estimate $\boldsymbol{\theta}+\delta \boldsymbol{\theta}$, computed as:

$$
\begin{equation*}
\underset{\boldsymbol{\theta}}{\operatorname{argmin}} E(P, B(l, \mathbf{r}), \boldsymbol{\theta}) \approx \underset{\delta \boldsymbol{\theta}}{\operatorname{argmin}} E(P, B(l, \mathbf{r}), \boldsymbol{\theta}+\delta \boldsymbol{\theta}) \tag{5}
\end{equation*}
$$

which is computed by taking:

$$
\frac{\partial E(P, B(l, \mathbf{r}), \boldsymbol{\theta}+\delta \boldsymbol{\theta})}{\partial \delta \boldsymbol{\theta}}=\mathbf{0}
$$

We finally get $\delta \boldsymbol{\theta}$ :

$$
\delta \boldsymbol{\theta}=-\left[J^{T} J+\lambda \operatorname{diag}\left(J^{T} J\right)\right]^{-1} J^{T} \mathbf{g}(\boldsymbol{\theta})
$$

where $J=\left[J_{1}, J_{2}\right], J_{i 1}=\frac{\partial d\left(p_{i}\right)}{\partial \theta_{1}}$ and $J_{i 2}=\frac{\left.\partial d\left(p_{i}\right)\right)}{\partial \theta_{2}}$ and $\mathbf{g}(\theta)$ is a column vector whose entries are $d(p, \boldsymbol{\theta})$ for each point $p$. $\lambda$ is a damping factor set to 0.01 initially and adapting it throughout iterations.

In the following, we assume $0<\tau_{\alpha}(p)<1$ and $n_{\tilde{p}} \cdot n_{p}>0$. In this case, $p$ projects on $\tilde{p}_{\alpha}$ and $d(p)=\left\|p p_{\alpha}^{\star}\right\|-r_{\alpha}(p)$ with $r_{\alpha}(p)=$ $\left(1-\tau_{\alpha}(p)\right) r_{1}+\tau_{\alpha}(p) r_{2}$, and $\tau_{\alpha}(p)=\frac{\left\|c_{1} p_{\alpha}^{\star}\right\|}{l}$. Hence:

$$
\begin{align*}
& \frac{\partial d(p)}{\partial \theta_{1}}=\frac{1}{\cos \alpha} \frac{\partial\left\|p^{\star} p\right\|}{\partial \theta_{1}}+\left(r_{2}-r_{1}\right) \frac{1}{l}\left(\frac{\partial\left\|c_{1} p^{\star}\right\|}{\partial \theta_{1}}+\tan \alpha \frac{\partial\left\|p^{\star} p\right\|}{\partial \theta_{1}}\right)  \tag{6}\\
& \frac{\partial d(p)}{\partial \theta_{2}}=\frac{1}{\cos \alpha} \frac{\partial\left\|p^{\star} p\right\|}{\partial \theta_{2}}+\left(r_{2}-r_{1}\right) \frac{1}{l}\left(\frac{\partial\left\|c_{1} p^{\star}\right\|}{\partial \theta_{2}}+\tan \alpha \frac{\partial\left\|p^{\star} p\right\|}{\partial \theta_{2}}\right) \tag{7}
\end{align*}
$$

The full expression for the derivatives can be easily derived given the expressions for $\left\|p_{\alpha}^{\star} p\right\|,\left\|c_{1} p^{\star}\right\|,\left\|p^{\star} p\right\|$ above. The cases $\tau_{\alpha}(p)<0, \tau_{\alpha}(p)>1$ or $n_{\tilde{p}} \cdot n_{p}<0$ can be computed similarly.

## C. Optimization for a joint between two consecutive bones

Let us consider the geometric optimization of the center of the joint between two bones by optimizing the two-bones energy with respect to the lengths $l_{k}$ and $l_{k+1}$. Each length is optimized in turn, with a side-effect on the value of the other length. The two-bones energy can be expressed as a function of $l_{k}$ :

$$
\begin{equation*}
E_{(k, k+1)}\left(l_{k}\right)=\sum_{p \in P_{k}}\left\|\tilde{p}_{k}-p\right\|^{2}+\sum_{p \in P_{k+1}}\left\|\tilde{p}_{k+1}-p\right\|^{2} \tag{8}
\end{equation*}
$$

Following the Levenberg-Marquardt algorithm, at each iteration, each parameter $l_{k}$ is replaced by a new estimate $l_{k}+\delta l$ :

$$
\begin{equation*}
\underset{l_{k}}{\operatorname{argmin}} E_{(k, k+1)}\left(l_{k}\right) \approx \underset{\delta l}{\operatorname{argmin}} E_{(k, k+1)}\left(l_{k}+\delta l\right) \tag{9}
\end{equation*}
$$



Figure 2: Pairwise Optimization. With fixed extremities $c_{k}$ and $c_{k+2}$, the pair of bones $B_{k}$ and $B_{k+1}$ is first rotated around axis $c_{k} c_{k+2}$ in order to minimize the two-bones energy. Then the lengths of the bones $B_{k}$ and $B_{k+1}$ and their common radius $r_{k+1}$ are optimized successively. After these updates, the point-to-bone assignment is recomputed. As the process is repeated the distances are more accurate since the point-to-bone assignment becomes more meaningful.

By setting $\frac{\partial E_{(k, k+1)}\left(l_{k}+\delta l\right)}{\partial \delta l}=0$, we get:

$$
\begin{equation*}
\delta l=-\frac{\sum_{p \in P_{k}} d_{k} \frac{\partial d_{k}}{\partial l_{k}}+\sum_{p \in P_{k+1}} d_{k+1} \frac{\partial d_{k+1}}{\partial l_{k}}}{\sum_{p \in P_{k}}\left(\frac{\partial d_{k}}{\partial l_{k}}\right)^{2}+\sum_{p \in P_{k+1}}\left(\frac{\partial d_{k+1}}{\partial l_{k}}\right)^{2}} \tag{10}
\end{equation*}
$$

where $d_{k}=\left\|p-\tilde{p}_{k}\right\|$ and $d_{k+1}=\left\|p-\tilde{p}_{k+1}\right\|$ are expressed as functions of $l_{k}$.

Let us detail the expression of $d_{k}$ with respect to $l_{k}$ : during the pairwise optimization $c_{k}$ and $c_{k+2}$ remain fixed (Figure 2). Let $c_{k}$ be the origin of a local reference frame with the x -axis aligned with $c_{k} c_{k+1}$. In this frame, the coordinates write $c_{k}(0,0,0), c_{k+1}\left(l_{k}, 0,0\right)$ and $c_{k+2}\left(x_{2}, y_{2}, z_{2}\right)$ while a point $P$ has coordinates $(x, y, z)$. Then $c_{k+1} c_{k+2}=\left(x_{2}-l_{k}, y_{2}, z_{2}\right), c_{k+1} p=\left(x-l_{k}, y, z\right)$.

Let us assume that $p$ projects on $\tilde{p}_{\alpha}$ (the case $\tilde{p}_{-\alpha}$ can be deduced with minor changes). Using the same notation as in Figure 1 and appendix B , recall that $d_{k}=\left\|p-\tilde{p}_{k}\right\|=\left\|p p_{\alpha}^{\star}\right\|-r_{\alpha}(p)$. Since when optimizing $l_{k}$ the orthogonal projection on $c_{k} c_{k+1}$ does not change, $\left\|p p^{\star}\right\|$ remains the same. However both $\alpha$ and $r_{\alpha}(p)$ change. Since $r_{\alpha}(p)=\left(1-\tau_{\alpha}(p)\right) r_{k}+\tau_{\alpha}(p) r_{k+1}$ with $\tau_{\alpha}(p)=$ $\frac{\left\|c_{k} p_{\alpha}^{\star}\right\|}{l_{k}}$, we get:

$$
\begin{equation*}
\frac{\partial d_{k}}{\partial l_{k}}=-\frac{\left\|p p^{\star}\right\|}{\cos ^{2} \alpha} \frac{\partial \cos \alpha}{\partial l_{k}}-\left(r_{k+1}-r_{k}\right) \frac{\partial \tau_{\alpha}(p)}{\partial l_{k}} \tag{11}
\end{equation*}
$$

Simple geometric considerations give $\cos \alpha=\sqrt{1-\frac{\left(r_{k+1}-r_{k}\right)^{2}}{l_{k}^{2}}}$, $\tau_{\alpha}(p)=\frac{\left\|c_{k} p^{\star}\right\|+\left\|p p^{\star}\right\| \tan \alpha}{l_{k}}$ and $\tan \alpha=\frac{r_{k+1}-r_{k}}{\sqrt{l_{k}^{2}-\left(r_{k+1}-r_{k}\right)^{2}}}$, whose differentiation with respect to $l_{k}$ is easy.

One must also express distances $d_{k+1}$ as functions of $l_{k}$. In that case, the projection on bone $B_{k+1}$ is slightly different, since the position of point $c_{k+1}$ changes with $l_{k}$. The formulas are only slightly modified by it, but this time $\left\|p p_{\star}\right\|$ also depends on $l_{k}$. We get:

$$
\begin{equation*}
\frac{\partial l_{k+1}}{\partial l_{k}}=\frac{1}{\cos \alpha} \frac{\partial\left\|p p^{\star}\right\|}{\partial l_{k}}-\frac{\left\|p p^{\star}\right\|}{\cos ^{2} \alpha} \frac{\partial \cos \alpha}{\partial l_{k}}-\left(r_{k+2}-r_{k+1}\right) \frac{\partial \tau_{\alpha}}{\partial l_{k}} \tag{12}
\end{equation*}
$$

The full expression for the derivatives can be easily computed using the following formulas:

$$
\cos \alpha=\sqrt{1-\frac{\left(r_{k+2}-r_{k+1}\right)^{2}}{\left(x_{2}-l_{k}\right)^{2}+y_{2}^{2}+z_{2}^{2}}}
$$

$$
\tau_{\alpha}(p)=\sqrt{\frac{\left(x-l_{k}\right)^{2}+y^{2}+z^{2}}{\left(x_{2}-l_{k}\right)^{2}+y_{2}^{2}+z_{2}^{2}}}
$$

$$
\left\|c_{k+1} p^{\star}\right\|=\frac{c_{k+1} p \cdot c_{k+1} c_{k+2}}{\left\|c_{k+1} c_{k+2}\right\|}=\frac{\left(x-l_{k}\right)\left(x_{2}-l_{k}\right)+y y_{2}+z z_{2}}{\left(x_{2}-l_{k}\right)^{2}+y_{2}^{2}+z_{2}^{2}}
$$

Plugging all the derivatives in Equation 10 yields $\delta l$, and $l_{k}$ can be updated as $\hat{l}_{k}=l_{k}+\delta l$. This impacts the position of $c_{k+1}$, whose new position is computed as $\hat{c}_{k+1}=c_{k}+\hat{l}_{k} \frac{c_{k} c_{k+1}}{c_{k} c_{k+1}}$, and $l_{k+1}$ is recomputed as : $l_{k+1}=\left\|\hat{c}_{k+1} c_{k+2}\right\|$.

The two-bones energy $E_{k, k+1}$ is then optimized with respect to $l_{k+1}$. This optimization is symmetric to the $l_{k}$ case above and can be easily adapted. Finally, the optimization of the radius of the common joint and rotation angle around axis $c_{k} c_{k+2}$ are done in a similar manner.

## D. Importance of the optimization order for registering a chain of bones.

During our optimization process our approach takes advantage of the articulated property of our model by processing bones in a specific order. Here, we run an experiment to illustrate that the order in which the optimizations are made is crucial.

To do so, we replace our iterations of sequential optimizations followed by point to bone reassignment by iterations of simultaneous parameter optimizations followed by point reassignment. At each iteration, the positions of all the joints are simultaneously optimized by minimizing their two-bone energies as if the adjacent joints remained fixed. The free joints at the extremities are also optimized at the same time by minimizing their one-bone energy as if their non free joint remaining fixed. However the parameter and pose change is not applied right away after each optimization but simultaneously once all updates have been computed.

If this optimization is run after our forward step (which is useful to bring each bone close to relevant data), it takes 43 iterations to converge, against 9 iterations only with our approach (See Figure 3 for an illustration of the stages). On the contrary, if the simultaneous optimization is run directly from the initial position, the method fails to converge. Figure 4 shows the result after 50 simultaneous optimizations steps.


Figure 3: Simultaneous Optimization for a chain of bones applied after the first Fakir forward pass. From left to right: initial position (after our forward step), position after 10 iterations, position after 35 iterations, position after convergence (43 iterations).


Figure 4: Simultaneous Optimization for a chain of bones applied directly from the initial position.


Figure 5: From left to right: Aphrodite statue, registration result without the normal-constrained projection, registration result with our normal-constrained projection

## E. Importance of the normal-constrained projection

In this section we demonstrate that the normal-constrained projection both improves the result of the registration and the computation time. It is especially true in the case of the Aphrodite statue (Figure 5). Indeed, for this statue, the arms cling to the body which leads to wrong assignment of points when no normal information is used, yielding an unrealistic statue pose. The normal-constrained projection, on the contrary, permits to recover a good pose of the arms. Furthermore, it takes $16.9 s$ and 2 iterations for the algorithm using normal-constrained projection, against $32.8 s$ and 8 iterations to converge to a wrong registration - otherwise (number of points: 38954). On simpler cases, like the Dancing Faun (see the main paper for a rendering of the shape), both methods manage to converge to the correct registration, but the computation time and number of iterations are still lower for the normal-constrained projection ( $8.7 \mathrm{~s}, 6$ iterations) than for the simple orthogonal projection ( 10.4 s , 10 iterations).


Figure 6: From left to right: the Dancer with Crotales statue, initialization position at bounding box center of point cloud, automatic registration result.


Figure 7: A failure case for automatic initialization. From left to right: the Victoria from TOSCA data set, initialization position at bounding box center of point cloud, automatic registration result.

## F. Automatic initialization test

Our attempt to automatically initialize FAKIR by placing the pelvis in the center of the bounding box is effective for many statues. The Figure 6 illustrates that this works with a vertically oriented statue, while the Figure 7 shows a failure result, due to the fact that the center of the bounding box does not give any information about the orientation of the body. Thus the chains of bones are not aligned with the appropriate points, which leads to a local minimum. An improved version using principal component analysis of the points to initialize the orientation of the pelvis and adding loose constraints on the length of the bones could improve the registration.

## G. Additional registration results

We show on Figures 8 and 9 four additional results, including one with a missing part (the arm) and some garments which do not hinder the registration. The Goddess Parvati and the Gorilla show the good performance of FAKIR on data which do not have realistic human proportions, while still using the standard human skeleton presented in the paper.
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Figure 8: Additional statue registration results. Top-left: Wounded Amazon (Rome, 150 A.D., Nye Carlsberg Glyptotek, Copenhagen, Denmark); Top-right: Age of Bronze (Auguste Rodin), top-right; Bottom: The Goddess Parvati (South India, Circa 1200 A.C.). For each result, we show the initial point set, overlay of the data and the registered model, and the registered model alone.


Figure 9: Additional result on the Gorilla from the TOSCA dataset (initial point set; overlay of the data and the registered model; registered model alone).

