



**Tutorial T2**  
**« Modeling Individualities in Groups and Crowds »**  
**Part**  
**« Individualized versus collective behaviours »**


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Tutorial T2 "Modeling Individualities in Groups and Crowds"  
 Eurographics'09, Munchen, April 2009

## Summary



1. What is Bunraku ?
2. A quick introduction to crowd simulation
3. Macroscopic Models
4. Microscopic Models
5. Multilayered Models
6. Experimental studies
7. Conclusion & Perspectives



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## What is Bunraku ?

A research team funded by five research organisms

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## A joint scientific objective

Perception, decision and action of real and virtual humans in virtual environments and impact on real environments




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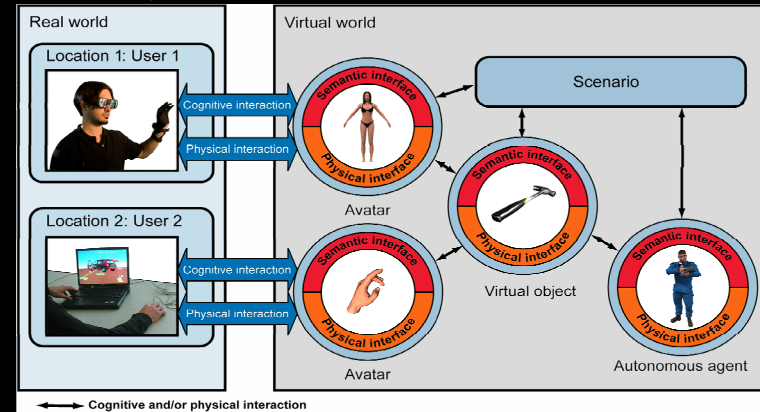
## Team Composition in october 2008

- 3 Professors: B. Arnaldi, K. Bouatouch, Y. Beckers
- 3 Researchers: S. Donikian, A. Lécuyer, J. Pettré
- 6 Assistant Professors: R. Cozot, T. Duval, G. Dumont, V. Gouranton, F. Lamarche, M. Marchal
- 2 Visiting Researchers: S. Gibet, M. Christie
- 2 Collaborators: F. Multon, R. Kulpa
- 2 Research Engineers: A. Chauffaut, C. Bouville
- 3 Post-doc: N. Ouarti, Z. Gao, T. Regia Corte
- 18 PhD students
- 6 Technical staff
- Total : 45



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## Overall Objective of our Research Team



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## Our challenges

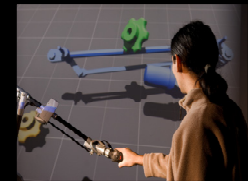
- Increase cross fertilization between two complementary research thematics
  - Virtual Reality and Virtual Humans
- Allow Real and Virtual Humans to naturally interact in a shared virtual world
- Combine two kinds of interaction of different nature: cognitive and physical



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## Complementary Research Thematics

- Multimodal Interaction with objects within the world
  - A generic multilevel model of an object
  - Multimodal rendering
    - visual, haptic, audio, cognitive
  - Acting on the objects of the world
    - language, gesture, mind
- Expressive Autonomous Characters
  - Complex and believable movements for human-like characters
  - Unified architecture to model individual and collective human behaviors
- Interactive scenario languages



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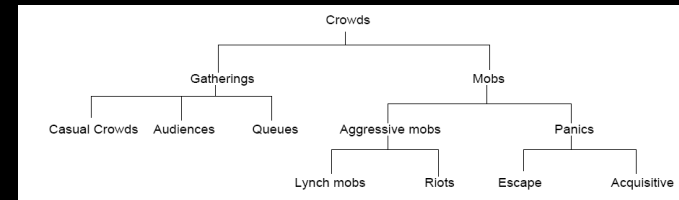
## A quick Introduction to crowd simulation



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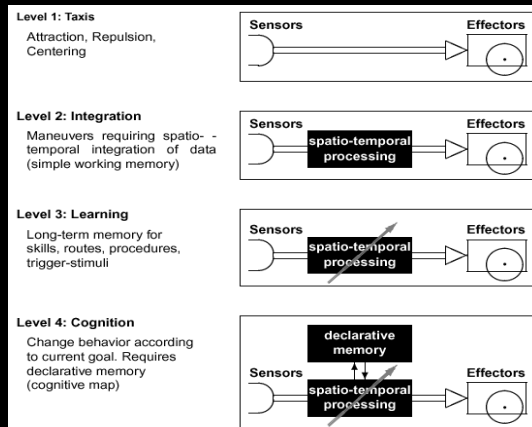
## Crowd definition

- Group: any gathering of two or more persons
- Mass: a large group
- Crowds: large groups that occupy a single location and share a common focus [Forsyth99]



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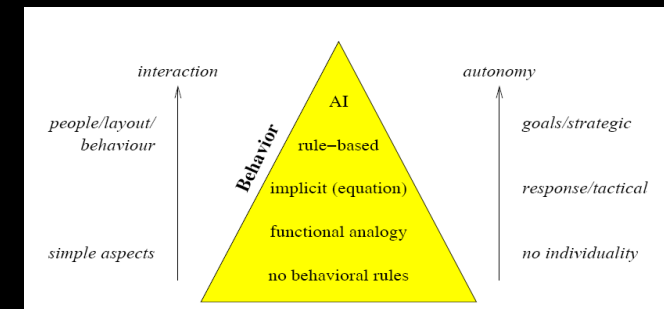
## Behavioral model classification [Mallot99]



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## Behavioral model classification [Klöpffel03]

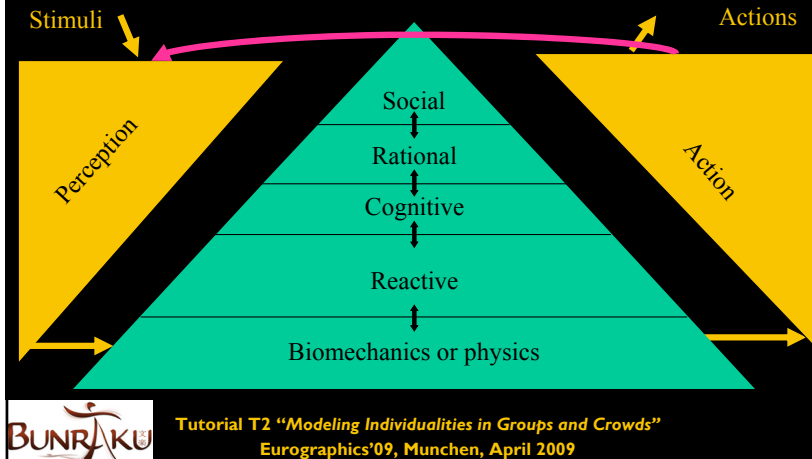
[Klöpffel03]



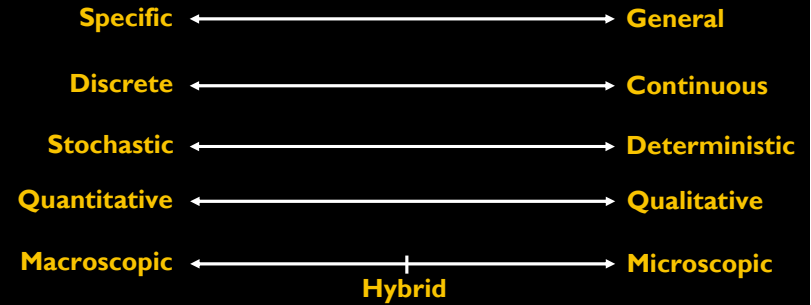
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## Behavioral model classification

[Donikian04]



## Models for Crowd Simulation



## Macroscopic Models



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## Macroscopic Models

- In this approach the pedestrian is not treated on its own but as a component of a more macroscopic element.
  - Statistical approach
  - Dynamics models (gas, fluid)

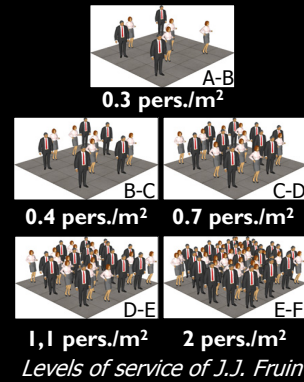


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## Levels of service (LOS) [Frui71]

- Based on real data collect
  - flow rate =  $f(\text{density})$

Level of service	Density		Flow rate
	pers./m <sup>2</sup>	m <sup>2</sup> /pers.	pers./min/m
A	< 0.3	> 3.2	< 23
B	[0.3, 0.4[	]2.3, 3.2]	[23, 33[
C	[0.4, 0.7[	]1.4, 2.3]	[33, 49[
D	[0.7, 1.1[	]0.9, 1.4]	[49, 66[
E	[1.1, 2[	]0.5, 0.9]	[66, 82[
F	≥ 2	≤ 0.5	variable

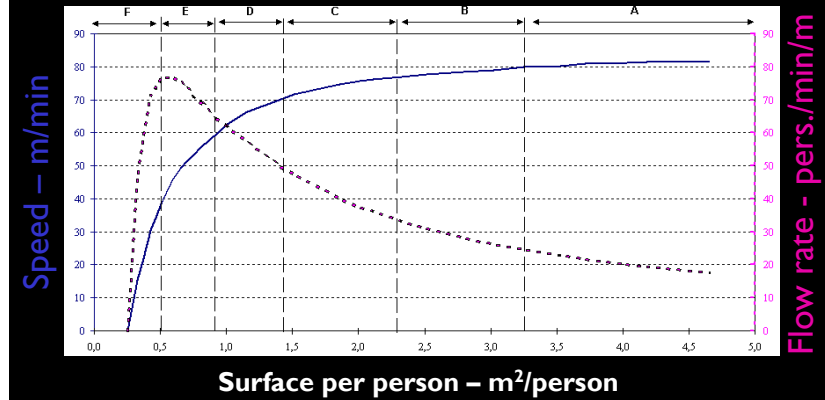


- Many variants [Puskarev77, Polus83, Tana89, Brilon94, Milazzo99]
  - Sociocultural Influence



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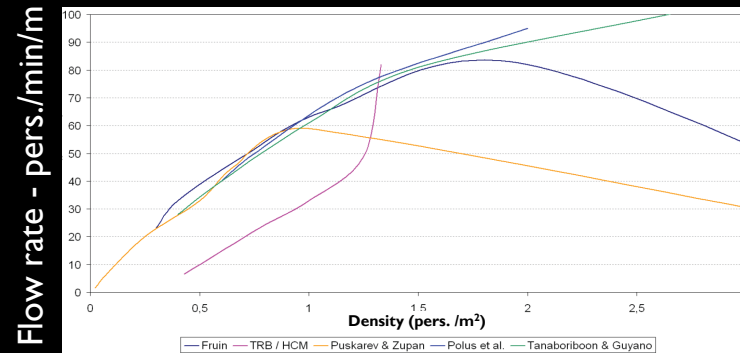
## Relation between density, possible speed and flow rate



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## Big disparity between models

- Model completely related to the observed situation, different for each model => a need for standardization



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## Macroscopic Simulation of crowds

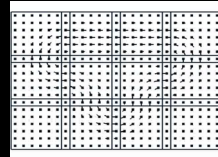
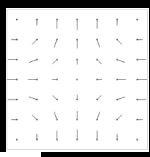
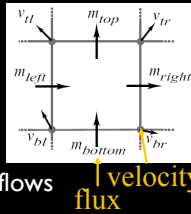
- Gaseous Model for low density [Henderson71]
  - Use of the Maxwell-Boltzmann Theory
  - Three possible states (stop, walk, run)
  - Distribution of velocities is Gaussian
- Hydraulic Model for high density [Archea79, Predtechenskii78]
  - The motion of persons in corridors, stairways and doors is assimilated to the one of water inside pipes and sluice-gates
  - Uniform distribution of persons inside pipes
  - Uniform flow rates and unidirectional flows
- Partial differential Equations are used in both cases to explain how crowd density and velocity are evolving.



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## Macroscopic Simulation of crowds [Chenney04]

- Flow tiles provide a set of flow fields that can be combined together to form large tilings.
- A tiling selection algorithm works on any mesh of edges, allowing to generate divergence-free flows
- Flow tiles drive the crowd using the velocity to define the direction of travel for each member.



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## Statistical Models

- Statistical Models to determine the evacuation time of an area by separating horizontal and vertical circulation spaces
- The Togawa Model [Togawa55]

$$V = V_0 \cdot \rho^{-0.8}$$

Speed of the crowd function of the density

- With  $V_0 = 1.3 \text{ m}\cdot\text{s}^{-1}$ , and  $\rho = \text{density (person / m}^2\text{)}$

$$N = \rho \cdot V = V_0 \cdot \rho^{0.2}$$

- With  $N = \text{flow rate (person / s / m)}$ ,  $1.3 < N < 1.7$

$$T = \frac{P}{C_e \cdot \sum L_e} + \frac{L_h}{v}$$

- With  $T$  the evacuation time,  $P$  the number of persons in the building,  $L_e$  the width of circulation areas,  $C_e$  a flow rate (fixed at 1.3 pers./m/s),  $L_h$  the total length of evacuation path and  $v$  the evacuation speed (usually 0.6 m/s)



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## Statistical Models

- The Pauls Evacuation Model [Pauls75, Pauls84a, Pauls84b]

$$Q = 0.206 \cdot (L - 0.3) \cdot \left(\frac{P}{L - 0.3}\right)^{0.27}$$

- with
  - $Q$  the flow rate
  - $P$  the number of people to evacuate
  - $L$  the width of the stairway (- 0.3 m as people are not using the full width)
- The evacuation time  $T$  is driven by the following equation

$$\frac{L}{P} = 8040 \cdot T^{-1.37}$$



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## Microscopic Models



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## Microscopic Model

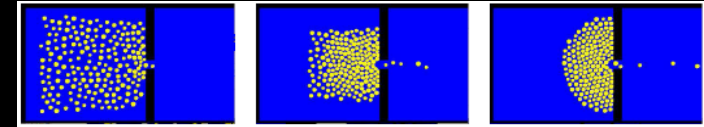
- Microscopic models consider persons as the elementary units of the model, and manage their interaction inside the environment.
- Different kinds of model
  - Particle systems
  - Cellular Automata
  - Predictive geometric models
  - Steering methods
  - Agent based approach



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## Particle System

- Introduced by I. Peschl in 1971 [Peschl71]
- Analogy between the displacement of persons in very dense area with the outflow of particles in a compartment
- Allow to model the agglutination phenomenon



- The probability of an arch appearance increases with the density
- The flow is linearly dependent of the exit width



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## Social Forces [Helbing95]

- Introduced by Dirk Helbing and Peter Molnar in 1995
- A social force is not a real force exerted by its surrounding on a pedestrian but rather a quantity that describes its motivation to act

$$\vec{F}_\alpha(t) := \overbrace{\vec{F}_\alpha^0(\vec{v}_\alpha, v_\alpha^0 \vec{e}_\alpha)}^{\text{Desired Motion}} + \overbrace{\sum_\beta \vec{F}_{\alpha\beta}(\vec{e}_\alpha, \vec{r}_\alpha - \vec{r}_\beta)}^{\text{Social Force}} + \overbrace{\sum_B \vec{F}_{\alpha B}(\vec{e}_\alpha, \vec{r}_\alpha - \vec{r}_B^a)}^{\text{Obstacle Avoidance}} + \overbrace{\sum_i \vec{F}_{\alpha i}(\vec{e}_\alpha, \vec{r}_\alpha - \vec{r}_i, t)}^{\text{Attractive Forces}}$$

Desired Motion Social Force Obstacle Avoidance Attractive Forces

- This model has evolved over the last decade with later contributions from Illes Farkas and Tamas Vicsek.



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## The Helbing-Molnar-Farkas-Vicsek Social Force Model [Helbing00]

- Each pedestrian feels and exerts on others two kinds of forces, social and physical.
  - Social forces (repulsion/attraction) reflect the intention of a pedestrian not to collide with others
  - Physical forces (pushing and friction) are used when pedestrian are forced to collide at very high density

$$\vec{f}_{ij} = \vec{f}_{\text{social repulsion}} + \vec{f}_{\text{pushing}} + \vec{f}_{\text{friction}}$$

$$\begin{aligned} \vec{f}_{\text{social repulsion}} &= A e^{(R_{ij} - d_{ij})/B} \vec{n}_{ij}, \\ \vec{f}_{\text{pushing}} &= k \eta(R_{ij} - d_{ij}) \vec{n}_{ij}, \\ \vec{f}_{\text{friction}} &= \kappa |\vec{f}_{\text{pushing}}| \vec{t}_{ij}, \end{aligned}$$

$A, B, k$ , constants

$\vec{n}_{ij}$ : vector  $\vec{ij}$

$\vec{t}_{ij}$ : tangential direction

$R_{ij}$ : sum of radii of  $i$  &  $j$

$d_{ij}$ : distance between  $i$  &  $j$

$$\eta(x) = \begin{cases} x, & x \geq 0; \\ 0, & x < 0. \end{cases}$$



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## The Helbing-Molnar-Farkas-Vicsek Social Force Model [Helbing00]

Force between a pedestrian  $i$  and an obstacle

$$\vec{f}_{io} = A e^{(r_i - d_{io})/B} \vec{n}_{io} + k \eta(r_i - d_{io}) \vec{n}_{io} + \kappa k \eta(r_i - d_{io}) \vec{v}_{io}$$

Force corresponding to preferred velocity of a pedestrian

$$\vec{f}_{\text{preferred}} = -m \frac{\vec{v} - \vec{v}_0}{\tau}, \quad \vec{v}_0 = (1 - p) V_0 \vec{e}_i + p \langle \vec{v}_j \rangle_i$$

It is a weighed average between his "own" velocity and a "collective" velocity that he perceives around himself

$$\frac{d\vec{x}_i(t)}{dt} = \vec{v}_i(t) \quad \vec{x}_i \quad \vec{v}_i \quad m_i \quad \text{Position, velocity and mass of pedestrian } i$$

$$m_i \frac{d\vec{v}_i}{dt} = \vec{f}_i(t) + \vec{\xi}_i(t) \quad \vec{\xi}_i(t) \quad \vec{f}_i(t) \quad \text{Fluctuation in panic situation}$$

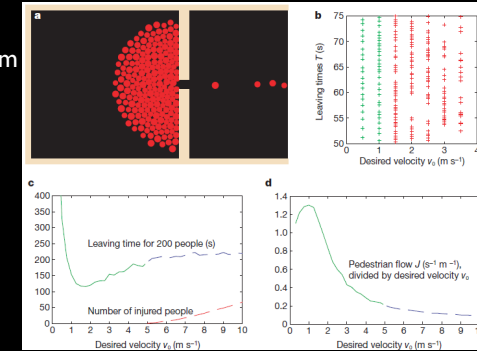
Sum of the preceding forces



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## Illustration of the HMFV Model in Normal and Evacuation Situations

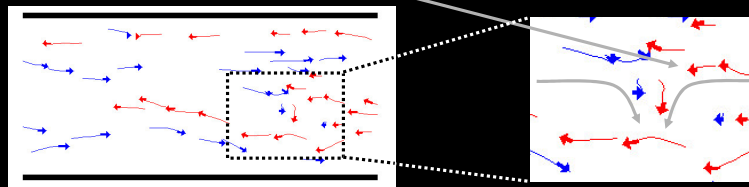
- Simulation of pedestrians moving with identical desired velocity
- 1m wide exit
- Room size 15m x 15m
- [Helbing01]



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## Illustration of the HMFV Model in Normal and Evacuation Situations

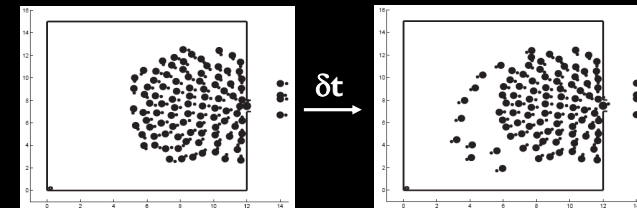
- Typical usage (validated):
  - high densities of people, evacuation scenarios
- Major problem:
  - lack of anticipation



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## Illustration of the HMFV Model in Normal and Evacuation Situations

- The validity domain is limited to very high densities
- Trajectories are not correct for individual pedestrians in sparse conditions.
- Problems may also arise at the boundary of the crowd



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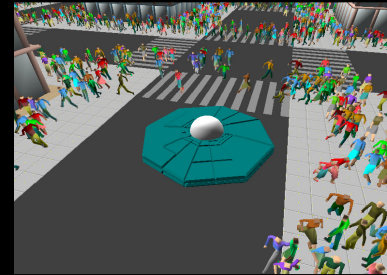
## The Lakoba-Kaup-Finkelstein Model [Lakoba05]

- Modification of the Helbing-Molnar-Farkas-Vicsek Social Force Model
  - To increase its domain of validity for lower densities
  - To eliminate overlapping between pedestrians
    - Stable solutions using the explicit 1<sup>st</sup>-order Euler Method
  - To add a memory providing to a pedestrian the knowledge about the location of exit(s)
    - Determines the vector of its preferred velocity



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## Potential fields [Treuille06]



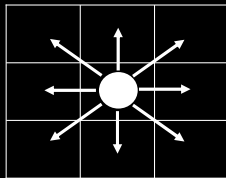
- Based on global attraction / repulsion forces
  - High performances
- Major problems:
  - unrealistic speeds
  - lack of control over individual destinations



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## Cellular Automaton [Schadschneider01]

- Discrete approach
  - use of a regular lattice, each cell approximately 40 x 40 cm<sup>2</sup>
  - Each cell is either empty or occupied by exactly one person



$P_{-1,1}$	$P_{0,1}$	$P_{1,1}$
$P_{-1,0}$	$P_{0,0}$	$P_{1,0}$
$P_{-1,-1}$	$P_{0,-1}$	$P_{1,-1}$

- $P_{i,j}$ : probability to go in the cell  $(x+i, y+j)$ : preferred walking direction
  - $\sum P_{i,j} = 1$
- In case of conflict (two particles share the same target cell), one is chosen according to their relative probabilities to choose the target



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## Cellular Automaton [Klüpfel03]

- A pedestrian can move more than one cell in a time-step  $\Delta t$
- Use of a time-step-slice  $\Delta t_s$ 
  - $\Delta t_s = \Delta t / v_{\max}$  ( $v_{\max}$  the maximum speed)
- For each time-step-slice:
  1. Try to access the desired cell
  2. If this is not possible, try to go to one of the two 45° neighbors
  3. If this is not possible, try to go to one of the two 90° neighbors
  4. If none of those five cells are accessible, then stop.
- The fact that diagonal movement corresponds to a longer distance is taken into account by a factor  $\sqrt{2}$



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## Floor Field [Schadschneider01]

- The floor field modifies the transition probabilities to increase the probability to move into the direction of larger fields.
- Dynamic floor field (Matrix  $D_{ij}$ ):
  - Used to model long-ranged attractive interaction between persons
  - Virtual trace are left by pedestrians, but they are subject to diffusion and decay
    - dilution until the vanishing of the trace after some time
- Static floor field (Matrix  $S_{ij}$ ):
  - Used to specify regions of space that are more attractive



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## Floor Field [Schadschneider01]

- The transition probability  $p_{ij}$  in direction  $(i, j)$  depends on four contributions:

$$p_{ij} = N P_{ij} D_{ij} S_{ij} (1 - n_{ij})$$

- With:
  - N: normalization factor to ensure  $\sum_{(i,j)} p_{i,j} = 1$
  - $n_{ij}$ : occupation number of the target cell (1 occupied, 0 free)
- Advantage:
  - simple, and can be used for large scale simulations



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## Example



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## CA + Social Distance [Was06]

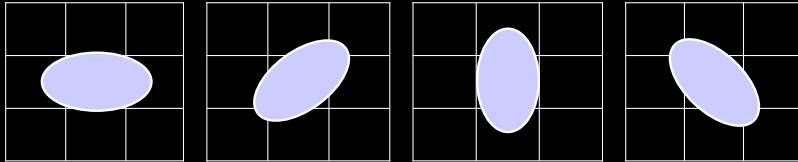
- Four sort of distances:
  - Intimate distance: below 40-50 cm
    - Can appear between couples, parents and children
  - Personal distance: from 40-50 cm to 150 cm
    - Close phase below 90 cm for people who know each other very well
  - Social distance: from 150 cm to 300 cm
    - Casual interaction-distance between acquaintances and strangers
  - Public distance: above 300 cm



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## CA + Social Distance [Was06]

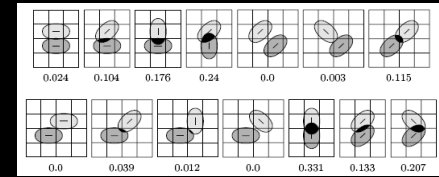
- Use of an elliptic body shape
  - $a = 0.225$  cm (semimajor axis) and  $b = 0.135$  cm (semiminor axis)
  - It is assumed the average size of a person (WHO data)
- Four allowed orientations in a cell



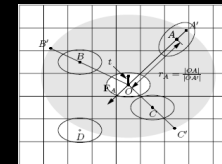
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## CA + Social Distance [Was06]

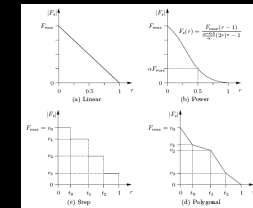
- A limited number of combinations



- Use of the social area ellipse (4a, 5b) and of social distance forces



in the example:  
 $F_s = F_A + F_B + F_C$



Different social distance force models



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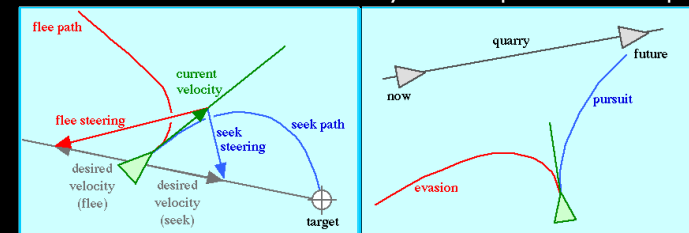
## Predictive methods



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## Steering Behaviors [Reynolds99]

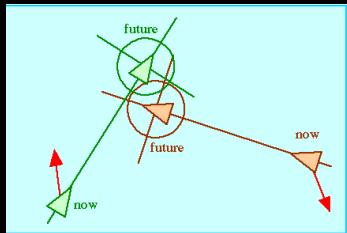
- Use of several different behaviors
  - Seek: steer the character towards a specified position
  - Flee: inverse of seek
  - Pursuit: identical to seek but with a moving target
  - Evasion: used to steer away from the predicted future position



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## Steering Behaviors [Reynolds99]

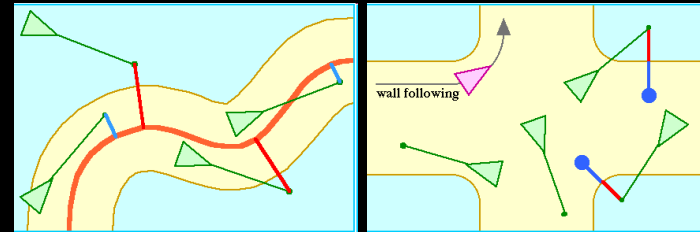
- Obstacle avoidance
- The obstacle which intersects the forward axis nearest the character is selected as the “most threatening.”
- Steering to avoid this obstacle is computed by negating the (lateral) side-up projection of the obstacle’s center.



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## Steering Behaviors [Reynolds99]

- Other behaviors



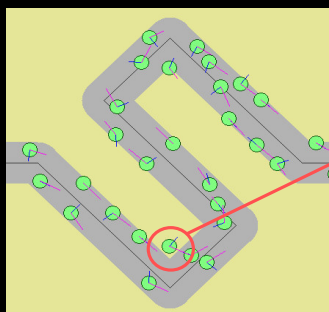
Path following

Wall following and containment



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## Steering Behaviors [Reynolds99]



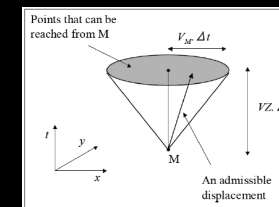
- Artifacts
- Major problem:
  - all the interactions must be described



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## Predictive Geometric Model [Feurtey00]

- Predictive approach to manage collision avoidance.
- Navigation of persons represented in a  $(x, y, t)$  reference system



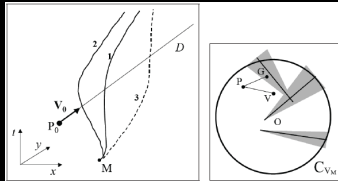
- At each time  $t$ , all possible positions that can be reached by a pedestrian are included in a circle of radius  $(V_M \cdot \Delta t)$  with  $V_M$  its maximal velocity.



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## Predictive Geometric Model [Feurtey00]

- A possible collision is represented in the cone by a segment in the case of an intersection with the trajectory of a surrounding entity.



- To manage the vagueness of the trajectory prediction, the potential collision area is extended to become a triangle.



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## Predictive Geometric Model [Feurtey00]

- Feurtey postulates that a person apply three rules with different priorities
  - Preserve its direction
  - Preserve its velocity
  - Preserve the time necessary for the displacement

- Those rules are synthesized in a cost function for each point  $P$  included in the circle of possible displacements of radius  $r_M$

$$C_P = K_1 \frac{GP}{2r_M} + K_2 \frac{\text{angle}(OV, OP)}{180} + K_3 \frac{|OP - OV|}{2r_M}$$

- With:

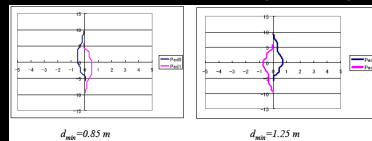
- $i = 3$  if  $OP \geq OV$  and  $i = 4$  otherwise
- $G$  the target location,  $K_1$  the cost of moving away from the goal,  $K_2$  the cost of changing direction,  $K_3$  the cost of acceleration,  $K_4$  the cost of deceleration



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## Predictive Geometric Model [Feurtey00]

- This approach has been tested only on tiny examples



- When many pedestrians need to be avoided, the disk may be saturated.
  - It is necessary to limit the number of pedestrians to take into account
- Oscillations may occur when two pedestrians are face to face



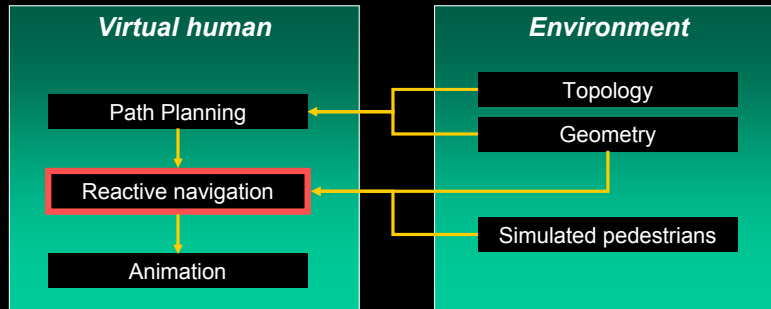
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## A new predictive reactive navigation algorithm [Paris07]



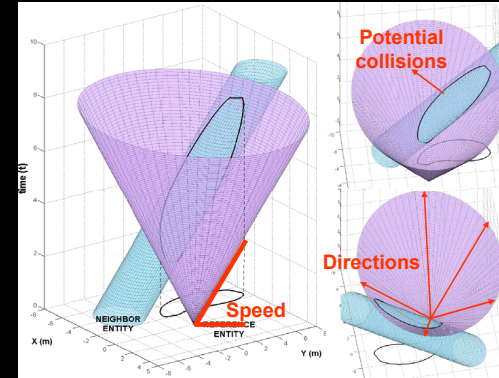
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## Part of a more complex virtual human presented hereafter



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## A predictive approach



- Reference entity
- Neighbor entity (position, speed)

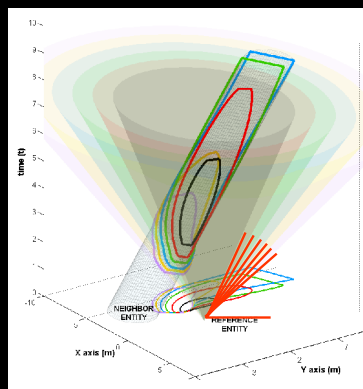
### Problem

How to choose a speed and direction to avoid all collisions in the near future?



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## A predictive approach



### Problem

Compute a cone/cylinder intersection.

### Solution

We choose a discrete model.



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## A discrete model Initial conditions

t=0  
Neighbor Entity  
(position, speed)

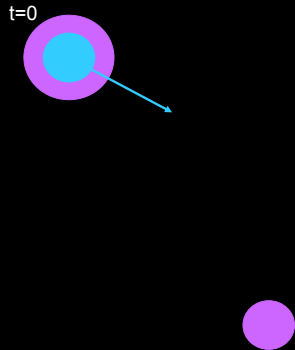
Direction / speed to avoid collision?

Reference Entity  
(position, goal)



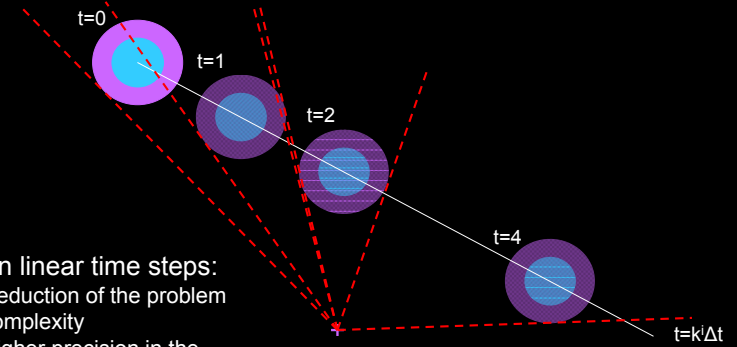
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## A discrete model Initial conditions



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## A discrete model Prediction



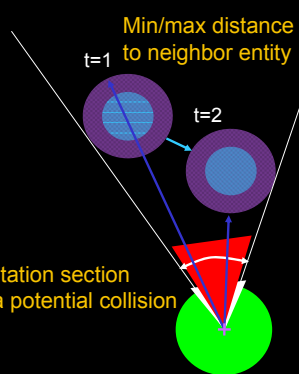
Non linear time steps:

- Reduction of the problem complexity
- Higher precision in the near future



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## Computation for each time interval



We deduce for each interval the critical speeds:

- The required fast velocity to get ahead of the neighbor
- The allowed slow velocity to move after the neighbor
- An analytic calculation is possible:

$$V_{slow} = \min_{t=t_1}^{t_2} \left( \left( \left\| \overrightarrow{P_r P_n(t)} \right\| - R \right) / t \right)$$

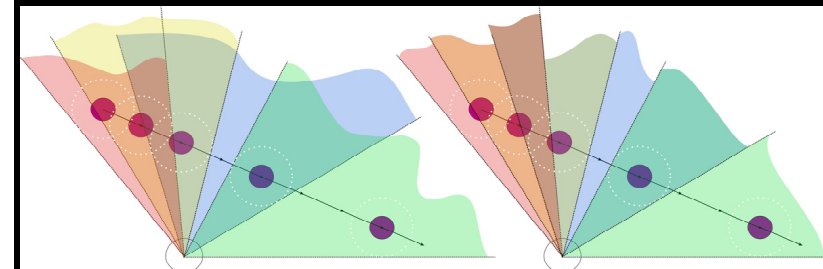
$$V_{fast} = \max_{t=t_1}^{t_2} \left( \left( \left\| \overrightarrow{P_r P_n(t)} \right\| + R \right) / t \right)$$

Orientation section  
with a potential collision



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## Merging the data of each overlapping section

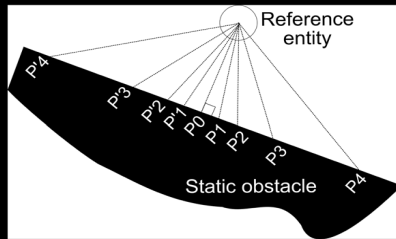


- Merging done for the intervals provided by:
  - One given neighbor entity
  - All entities taken into account



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## Taking into account the static obstacles



The same discrete approach as before is used:

- $V_{fast}$  is a nonsense
- The intervals are computed from the nearest point of the obstacle  $P_0$  to both of its edges



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## Selection of the best orientation and speed

- Computation of a weight for each section:
  - Reference entity: *goal, current state*
  - Section:  $V_{slow}, V_{fast}, orientations$
- The lower weight gives the best move.
- The cost function:
  - defines the realism level
  - requires a calibration phase: *experimental data are needed*



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## Simulation Results of the model



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## Need of social and group behaviours



[Raccourci vers compo-groupes.avi.link](#)

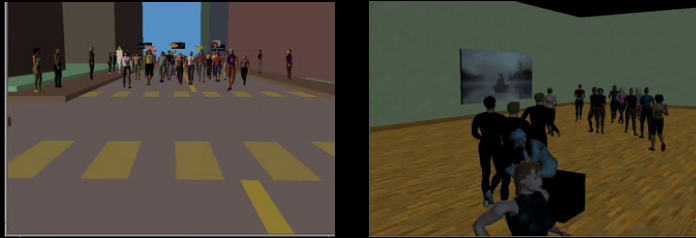


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## Group based crowd simulation [Musse99]

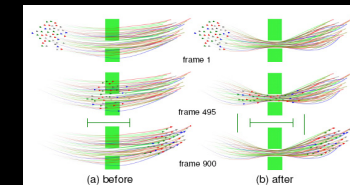
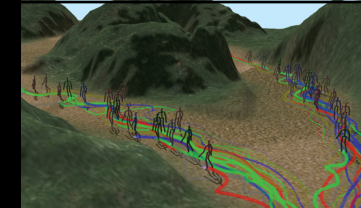
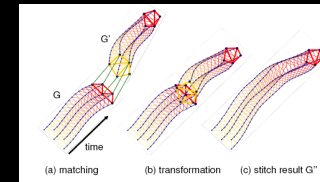
- Individual trajectories of virtual humans determined by the behaviour of the group they belong to.



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## Group Motion Editing [Kwon et al. 08]

- Provide an easy to use manner to control the trajectory of groups of people in a virtual environment.
- Edit
- Combine several spatial elements



Raccourci vers 0370.avi Link



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## Multi-layered Models



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## Multi-layer Approach

Dynamic approach in three layers [Goldenstein01]

- Particle based dynamic system
- Management of the relations between moving objects and the environment (based on Delaunay triangulation)
- Path planning and calculation of the desired orientation to reach a destination.



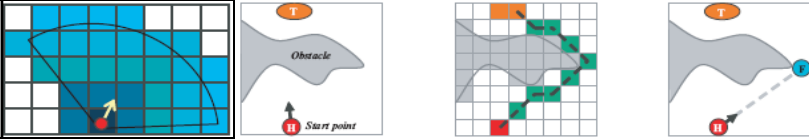
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# Autonomous pedestrians in a train station [Shao07]

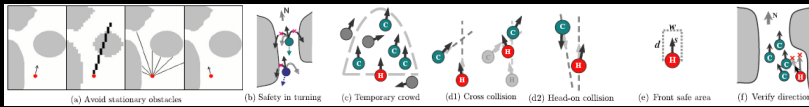
Raccourci vers Shao-terzopoulos1.avi.link

Raccourci vers Shao-terzopoulos2.avi.link

- Modelling of individual behaviours
- Use of a regular grid for reactive navigation and perception



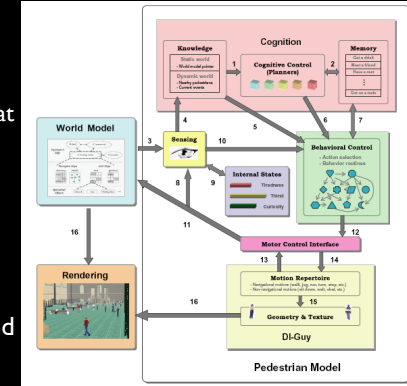
- Use of six basic reactive behavior routines



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# Autonomous pedestrians in a train station [Shao07]

- Motivational behaviors are used to supplement basic reactive routines, such as:
  - Meet with friends and chat
  - Queue at a ticketing area
- An action selection mechanism chooses the appropriate behavior to fulfill needs.
- A cognitive model is responsible for creating and executing plans suitable.



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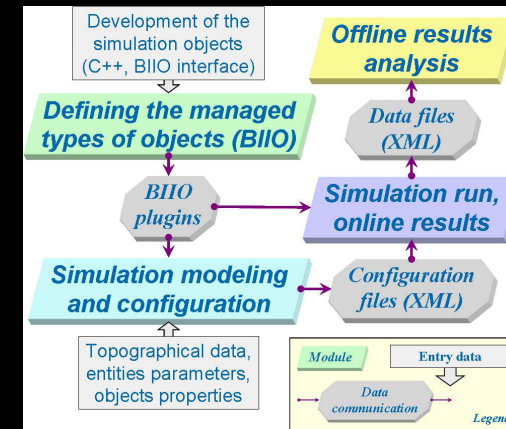
# A Goal Oriented Multi-layered Behavioral Simulator dedicated to Mobility Areas [Paris08]

- Objective
  - Develop the first goal oriented simulation tool
    - dedicated to train station and more generally to transportation terminals
    - including all the human activity inside this restricted area



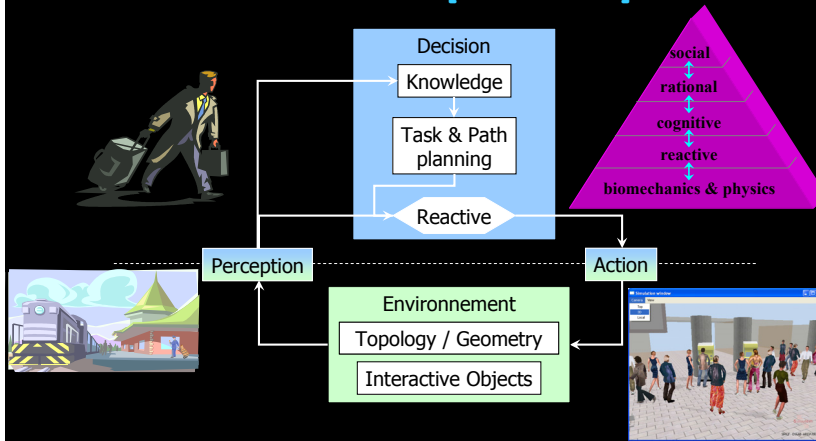
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# Simulator Architecture



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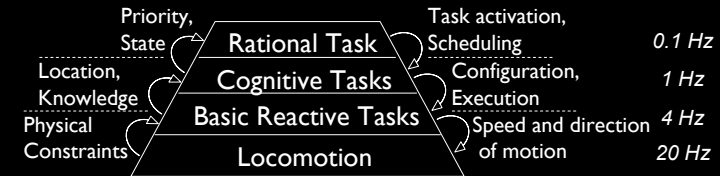
## Model Architecture [Paris PhD 07]



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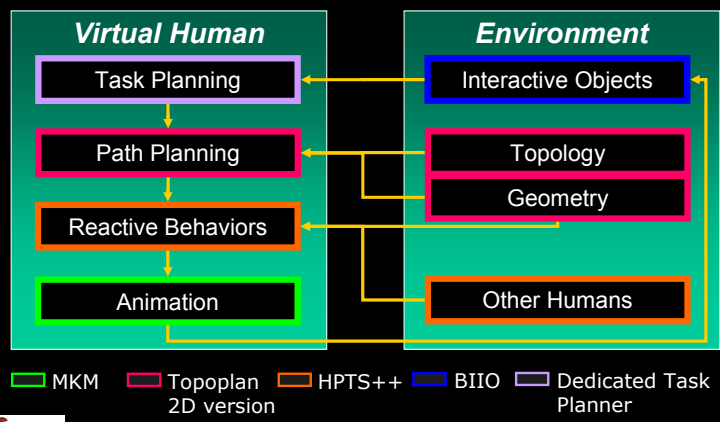
## An Embodied and Situated Virtual Human

- Based on the Behavioral Pyramid
  - All processes are independent and only connected to the connex layers



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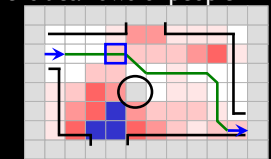
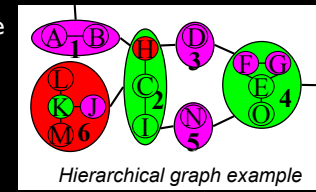
## Global crowd simulation architecture



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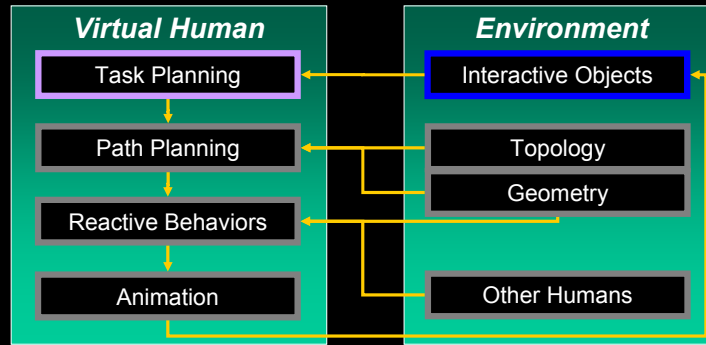
## Environment Representation [Paris06]

- Based on the exact geometry of the digital mockup (AutoCAD)
- Computation of a 3 layers hierarchical graph
- Pre computed data / computation procedures



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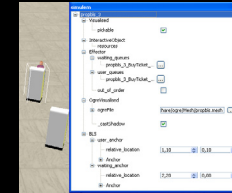
## Global crowd simulation architecture



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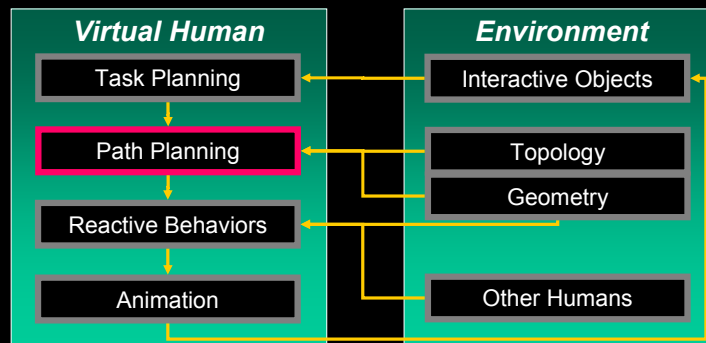
## Cognitive and Rational Tasks

- Cognitive Tasks
  - Concurrent Atomic Processes (priorities)
    - Interact: complete management of an affordance
    - Move: management of default displacement
    - Observe: management of visual attention
- Goal Oriented Rational Model
  - manage all affordances
    - Rational Process classifying all interactions
    - Hierarchical Organization of affordances



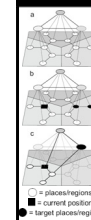
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## Global crowd simulation architecture



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## Path Planning: a Hierarchical Technique [Paris06]

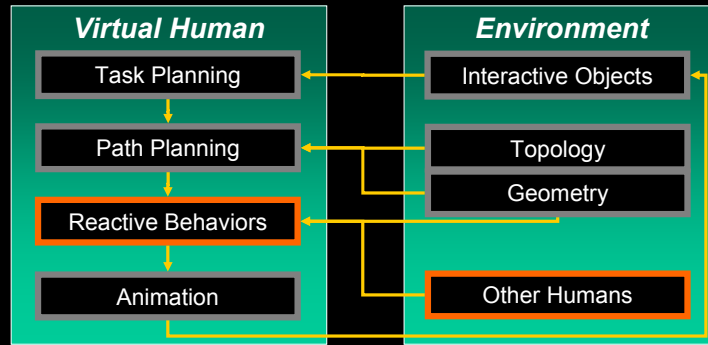


- Full path calculation in the more abstracted graph
  - To find an approximate path from current to destination zone
- By part calculation in the contained sub-graphs
  - Locally refine the path as the entity moves inside the environment
- 3 specializations for the full path calculation
  - Reach a unique identified target
  - Choose the best target between a set of identified ones
  - Explore: Reach a target which may improve the entity's knowledge of the environment
- Multicriteria Heuristic based on static data (path width & length, deviation angles, discovering potential) and dynamic data (densities and flows of people)



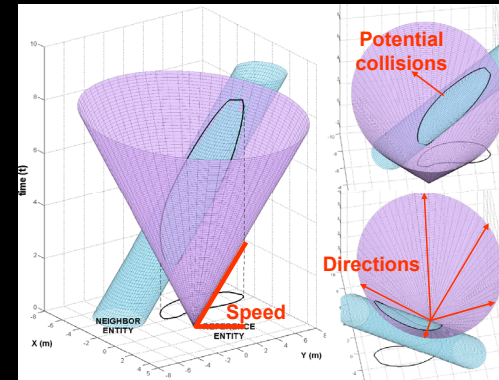
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## Global crowd simulation architecture



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## A predictive approach [Paris07]



■ Reference entity  
■ Neighbor entity  
(position, speed)

### Problem

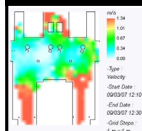
How to choose a speed and direction to avoid all collisions in the near future?



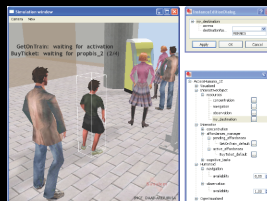
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## Simulation Characteristics

- Population generation based on exploitation data, distribution of delay before departure, Origin Destination Graph, ...



Mean Speed  
Spatial  
Distribution



Queuing up to buy a ticket



Each virtual human interacts with others but behaves depending on its own goals



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## Configuration of a simulation

- Population generation based on exploitation data, distribution of delay before departure, Origin Destination Graph, ...

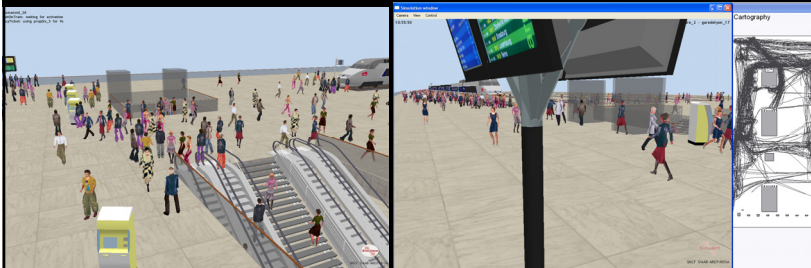
A screenshot of a simulation configuration window showing a table of parameters. The table has columns for Number, Departure Time, Arrival Time, From, To, Quality, Material, Population, Platform, and angles in degrees.

Number	Departure Time	Arrival Time	From	To	Quality	Material	Population	Platform	angles in degrees
1	10:56	10:54	MARSEILLE ST CHARLES	RENNES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100
2	12:14	11:18	LILLE EUROPE	RENNES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_2	100 100
3	10:56	10:51	PARIS	RENNES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100
4	10:57	10:52	BREST	PARIS	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100
5	10:58	10:53	TOLLOUZE MONTAUDOU	LILLE EUROPE	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100
6	11:18	10:56	LILLE EUROPE	NANTES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_2	100 100
7	12:00	11:27	RENNES	MARSEILLE ST CHARLES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100
8	12:21	12:18	LILLE EUROPE	RENNES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_2	100 100
9	12:21	12:18	LILLE EUROPE	NANTES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100
10	12:30	12:28	TOLLOUZE MONTAUDOU	RENNES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_2	100 100
11	12:48	12:45	MARSEILLE ST CHARLES	NANTES	QualityFGV_1	TGV_type1	Population_TGV1	Wag_1	100 100



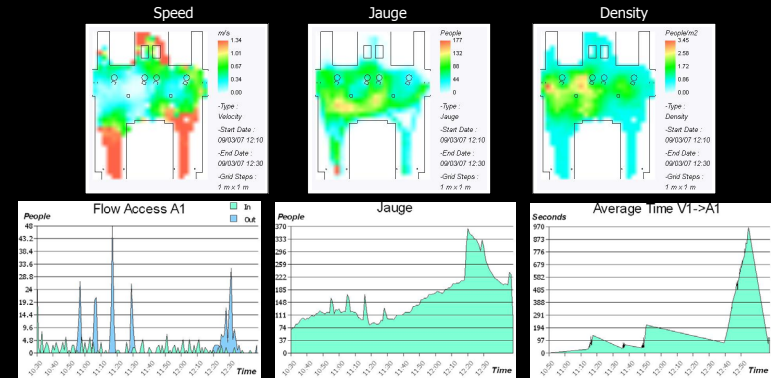
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## Running a simulation



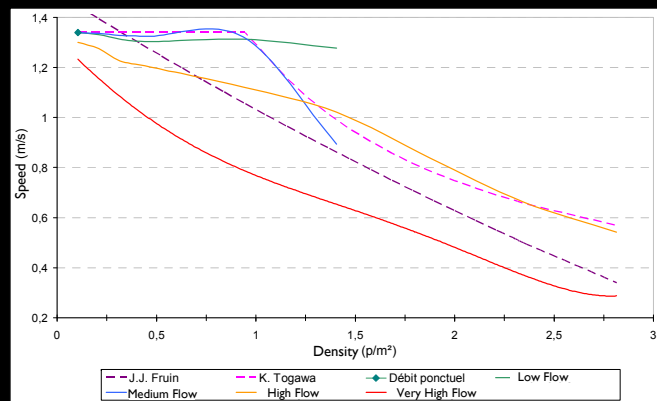
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## Exploitation of simulation results



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## Comparison with statistical models



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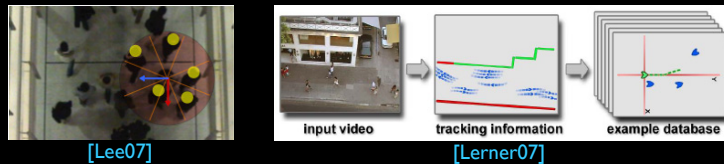
## Experimental studies



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## The Experimental Validation Problem

- Validate the proposed models
- Problem:
  - impossible to compare a virtual behavior with a real one on complex examples
- Solution:
  - Statistical validation based on macroscopic data or mean data
  - Use real data to calibrate the model



[Lee07]

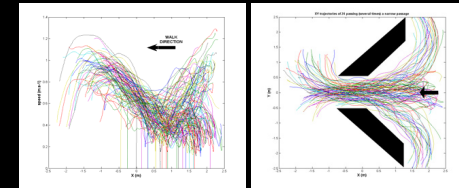
[Lerner07]



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## Experimental Studies

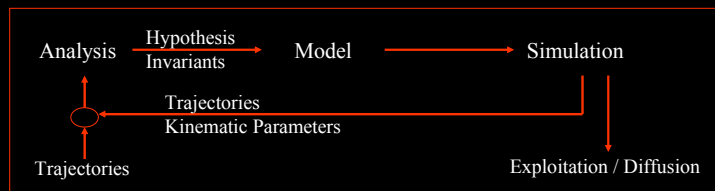
- Study interactions between two persons under different configurations
- Observation of micro-phenomena in micro-crowds



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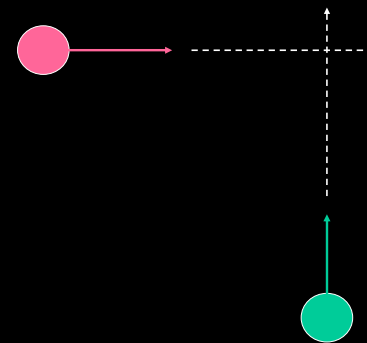
## Analysis and Synthesis Approach for Virtual Humans

- Use an Analysis/Synthesis approach to model human characteristics:
  - Locomotion, reactive navigation, path planning, ...



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## Experiments for Model Calibration Interaction with 2 subjects

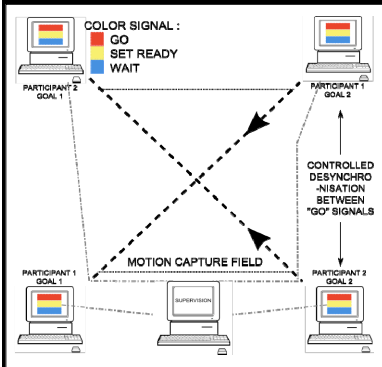


- Constrain trajectories to produce an interaction:
  - Geometrical
  - Temporal
- Goal:
  - Interaction condition ?
  - Avoidance strategy ?
- Technical method:
  - Motion capture



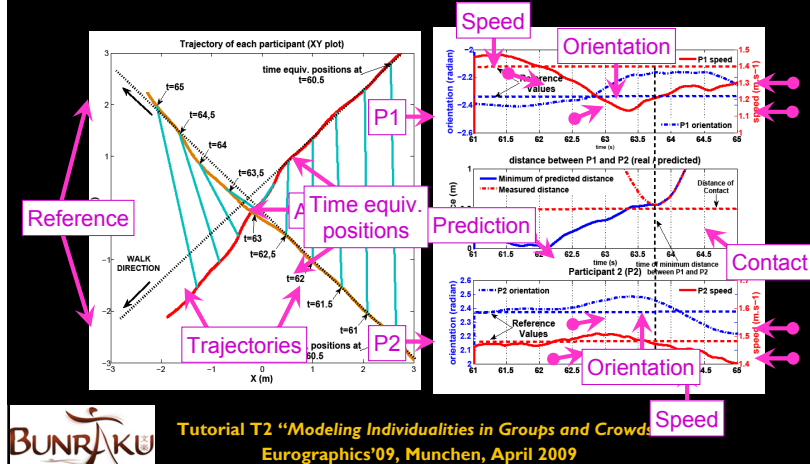
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## Experiments for Model Calibration Interaction with 2 subjects



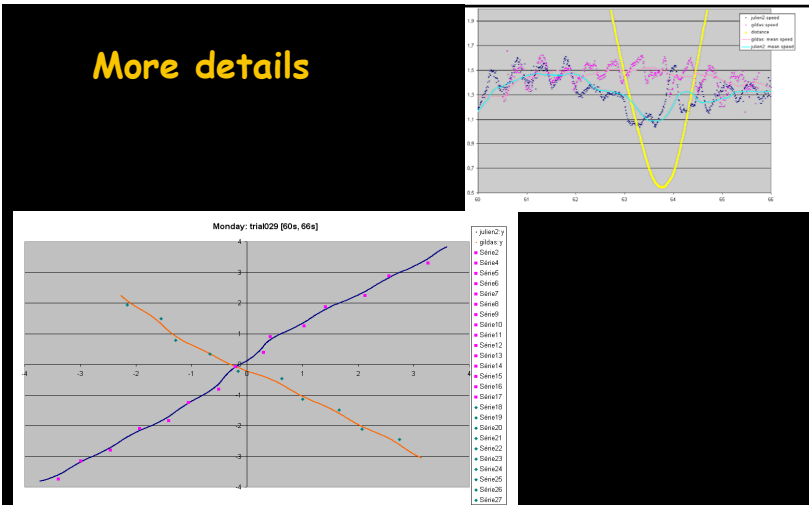
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## Experiments for Model Calibration Interaction with 2 subjects



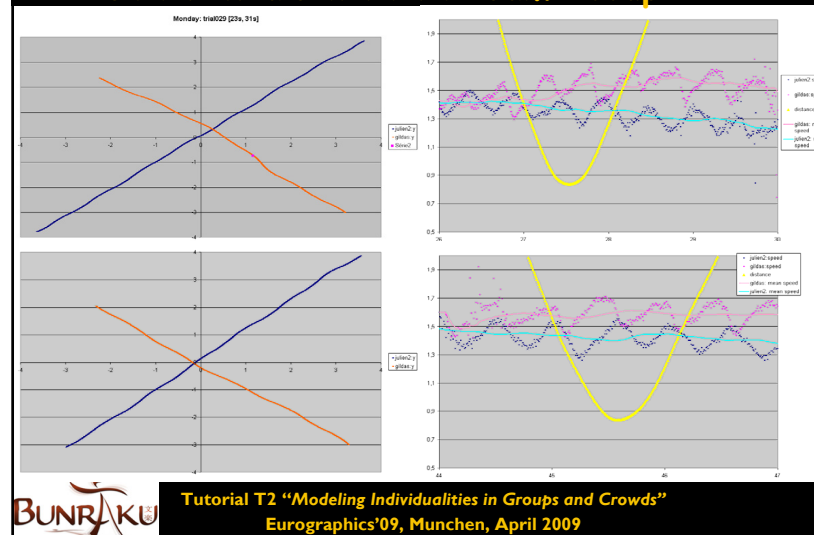
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## More details



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## Other trials with the same couple



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## Experiments for Model Validation Micro-crowd

### Problem

Do the rules which are observed for 2 subjects **remain valid** for more complex interactions?

### Solution

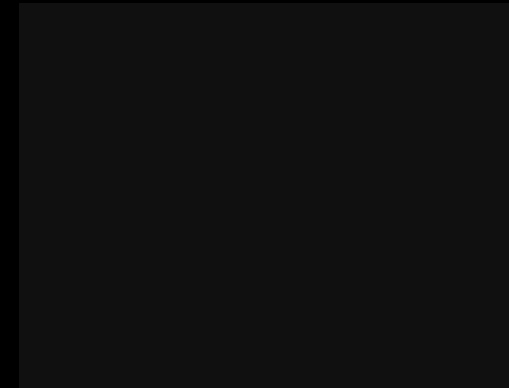
Observation of crowds **micro-phenomena** in « classical situations »

- Door crossing,
- Corridor,
- Crossroad,
- Etc.



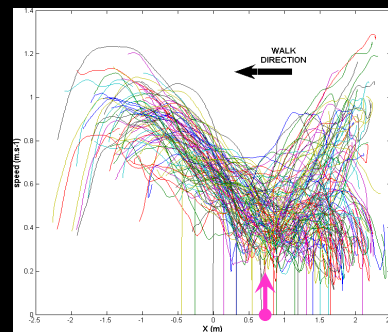
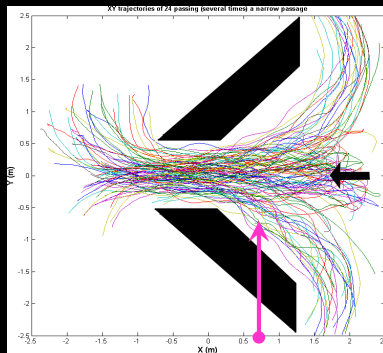
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## Experiments for Model Validation Micro-crowd



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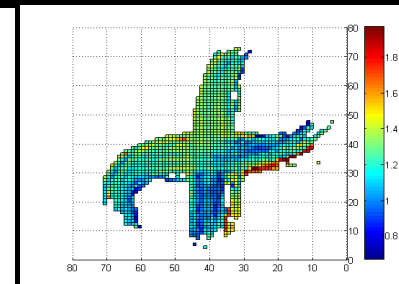
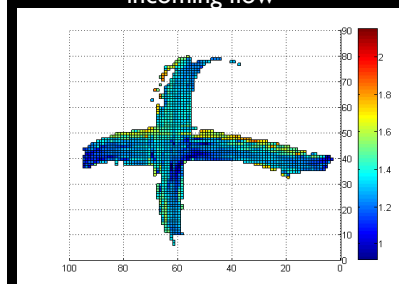
## Experiments for Model Validation Micro-crowd



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## Experiments for Model Validation Micro-crowd

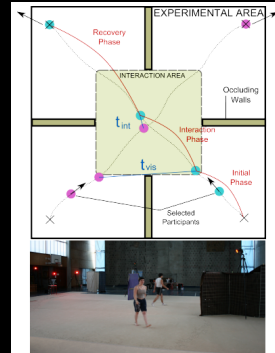
- Navigation in an area with obstacles
- Two scenarios: with or without visibility of the other incoming flow



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## Comparison of crowd simulation models with real data

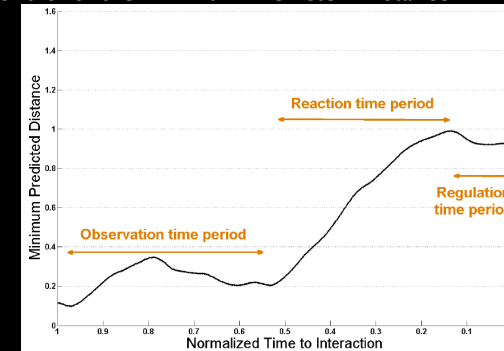
- Experimental square is 15m long, interaction area is 10m long.
- We randomize participants selection so that they cannot anticipate the direction from which one will appear.
- 429 experimental samples and 62 reference trajectories have been recorded.



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## An interaction in three steps

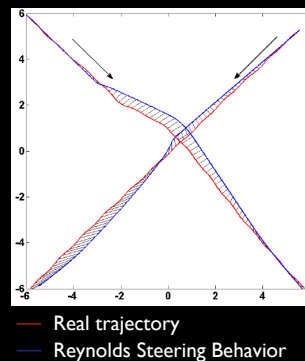
- Control of the Minimum Predicted Distance



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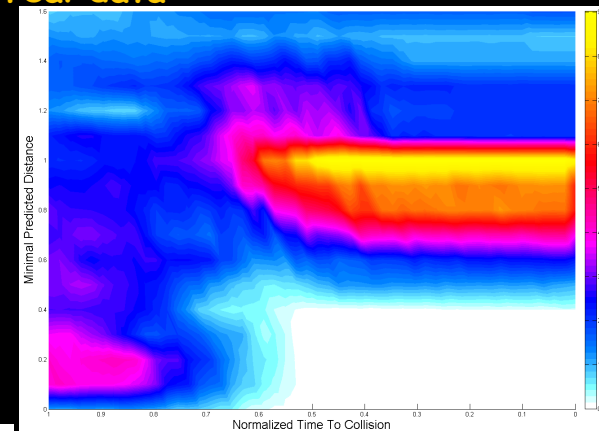
## Reynolds Steering Behavior [Reynolds99] vs real data

- The Reynolds' method converges toward a correct final distance between walkers.
- Reaction is too abrupt, as mpd is suddenly increased.
- Walkers adapt their motion simultaneously in this approach while in reality, adaptations are not synchronized.



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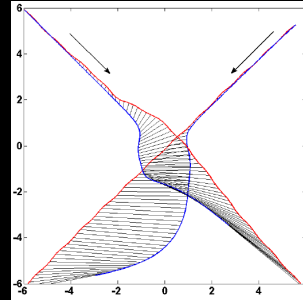
## Reynolds Steering Behavior [Reynolds99] vs real data



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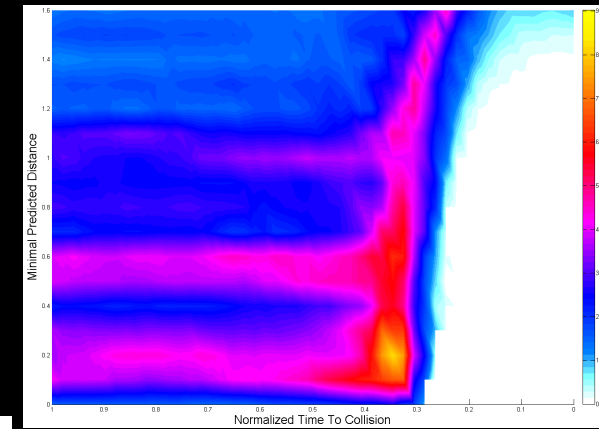
## Helbing Molnar Model [Helbing95] vs real data

- The lack of anticipation is clearly observable.
- The minimal distance between walkers is maintained over realistic values.



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## Helbing Molnar Model [Helbing95] vs real data



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## Conclusion

- Models of reactive navigation are usually reactive which is not sufficient at low density
- Models do not take into account several steps in the interaction
  - They are usually reacting too late and overmuch
- There is a need for a realistic predictive navigation model
- Recently, multi-layered models have been proposed allowing to combine reactive and cognitive behaviors increasing the realism of resulting simulations by providing goals and motivations to the virtual populace.



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## Open questions

- What is the model used by a pedestrian to adapt its trajectory to potential interactions with others ?
- Combination of speed and orientation adaptation due to the interaction with a subset of its neighbors
  - How is this combination ?
  - How are filtered the neighbors ? How many are they ?
- We are working in a pluridisciplinary project (Locanthrope) to answer these questions in a near future.



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The End!

Thank you for your attention

Questions ?



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